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Digital Design Using HDLs
LSU EE 4755
Midterm Examination
Wednesday, 19 October 2022, 11:30-12:20 CDT

Problem 1 _____ (25 pts)

Problem 2 _____ (31 pts)

Problem 3 _____ (20 pts)

Problem 4 _____ (12 pts)

Problem 5 _____ (12 pts)

Alias _____

Exam Total _____ (100 pts)

Good Luck!

Problem 1: [25 pts] Answer the following multiplexor questions.

(a) Complete module `mux4` so that it implements a 4-input multiplexor using instantiations of the 2-input multiplexor shown below. Do not use procedural code.

- Complete `mux4` so that it implements a 4-input multiplexor using `mux2` instantiations.
- Do not use procedural code. Do not change the ports or default parameters of `mux4` or `mux2`.
- Don't forget to declare any objects that are used.

```
module mux4
  #( int w = 3 )
  ( output uwire [w-1:0] x,
    input uwire [1:0] s,      input uwire [w-1:0] a0, a1, a2, a3 );
```

```
endmodule
```

```
module mux2
  #( int w = 6 )
  ( output uwire [w-1:0] x,
    input uwire s,      input uwire [w-1:0] a0, a1 );
  assign x = s ? a1 : a0;
endmodule
```

(b) Module `mux2_bad` only works for `w=1`. Describe the problem and show the correct mux output and the output of `mux2_bad` for `w=4`, `s=0`, `a0=2`, and `a1=4`.

```
module mux2_bad
  #( int w = 4 )
  ( output uwire [w-1:0] x,
    input uwire s,   input uwire [w-1:0] a0, a1 );
  assign x = !s && a0 || s && a1;
endmodule
```

- In `mux2` (a correct mux) when `w=4`, `s=0`, `a0=2`, and `a1=4`, output `x=`
- In `mux2_bad` when `w=4`, `s=0`, `a0=2`, and `a1=4`, output `x=`
- Explain the problem when `w` is not 1.

(c) Complete module `mux2_1r` below so that it recursively implements a 2-input w -bit mux. All that remains to be done is completing the connections to the two recursive instances, `m1` and `mr`.

```
module mux2_1r
  #( int w = 5 )
  ( output uwire [w-1:0] x,
    input uwire s,   input uwire [w-1:0] a0, a1 );

  if ( w == 1 ) begin
    assign x = !s && a0 || s && a1;
  end else begin

    mux2_1r #(1)   m1(

    mux2_1r #(w-1) mr(

  end

endmodule
```

Problem 2: [31 pts] The `val` output of `atoi_it_m_to_1` is the value of the radix-`r` ASCII-represented number appearing at its input, `str`, and output `nd` is the number of digits. Unlike the Homework 2 Problem 2 module, this module starts at the most-significant digit rather than the least-significant digit.

```

module atoi_it_m_to_1
  #( int r = 11, n = 5, wv = $clog2( r**n ), wd = $clog2(n+1) )
  ( output logic [wv-1:0] val,
    output logic [wd-1:0] nd,
    input uwire [7:0] str [n-1:0] );

  uwire [wv-1:0] vali[n:0];
  uwire is_digit[n:0];
  uwire [wd-1:0] ndi[n:0];
  assign is_digit[n] = 0;
  assign ndi[n] = 0;
  assign vali[n] = 0;
  assign nd = ndi[0];
  assign val = vali[0];

  localparam int wcv = $clog2(r);

  for ( genvar i=n-1; i>=0; i-- ) begin

    // Find Value of Digit i
    uwire [wcv-1:0] vald;
    atoi1 #(r,wcv) a( vald, is_digit[i], str[i] );

    // Multiply (scale) the accumulated sum.
    uwire [wv-1:0] valns;
    mult_by_c #( .w_in(wv), .c(r), .w_out(wv) ) mc( valns, vali[i+1] );

    // Update accumulated value.
    assign vali[i] = is_digit[i] ? valns + vald : 0;
    // Update number of digits.
    assign ndi[i] = !is_digit[i] ? 0 : is_digit[i+1] ? ndi[i+1] : i + 1;

  end

endmodule

```

(a) Describe how the behavior of the module would change if the loop direction were changed as shown below, but no other changes were made.

```

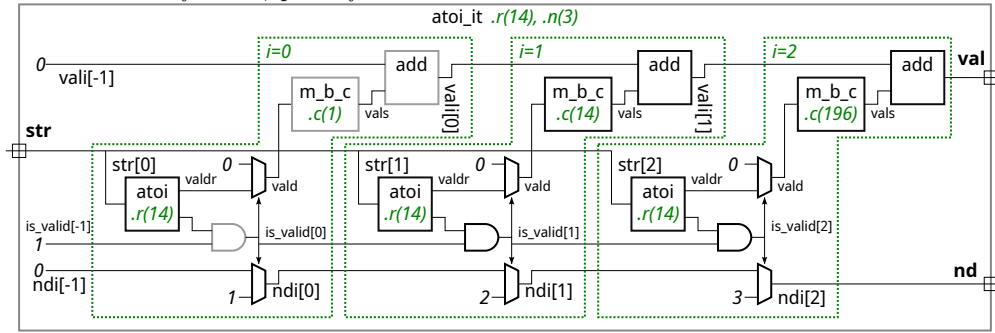
for ( genvar i=0; i<n; i++ ) begin

```

Change in behavior with ascending loop:

(b) On the next (facing) page show the hardware that will be inferred for an instantiation of `atoi_it_m_to_1` (descending loop version) with `n=3` and `r=10`. Show each instantiation of `atoi1` and `mult_by_c` as a box, do not show their contents. The inferred hardware for `atoi_it` is shown for reference.

For reference, part of Homework 3 Problem 2 solution shown below.



For reference, part of Homework 3 Problem 2 solution shown above.

- Show inferred hardware for `atoi_it_m_to_l` for `n=3` and `r=10`.
- Show the hardware inferred for the operators, such as `&&` and `?:`.
- Do not confuse parameters and ports and omit hardware that does not belong, such as “hardware” to compute values needed at elaboration time.

(c) Module `atoi_m_to_l` will only show the value of numbers that are right-aligned in `str`, otherwise the value will be shown as zero. For example, for input `str="--123"` the output would be `val=123` and `nd=3`, but for input `str="_123_"` the output would be `val=0` (because the rightmost character is not a digit). Modify the module so the `val` output is the value of the number regardless of its location. If there is more than one number, say `str="--12_345_"`, show the value of the rightmost number, 345 in this case.

- Modify so that `val` and `nd` are for numbers whether or not they are right-aligned.
- Do not use procedural code.
- Avoid costly or slow solutions.
- A correct solution only requires a few changes.

```

module atoi_it_m_to_l
  #( int r = 11, n = 5, wv = $clog2( r**n ), wd = $clog2(n+1) )
  ( output logic [wv-1:0] val,
    output logic [wd-1:0] nd,
    input uwire [7:0] str [n-1:0] );

  uwire [wv-1:0] vali[n:0];
  uwire is_digit[n:0];
  uwire [wd-1:0] ndi[n:0];
  assign is_digit[n] = 0;
  assign ndi[n] = 0;
  assign vali[n] = 0;
  assign nd = ndi[0];
  assign val = vali[0];

  localparam int wcv = $clog2(r);

  for ( genvar i=n-1; i>=0; i-- ) begin

    // Find Value of Digit i
    uwire [wcv-1:0] vald;
    atoi1 #(r,wcv) a( vald, is_digit[i], str[i] );

    // Multiply (scale) the accumulated sum.
    uwire [wv-1:0] valns;
    mult_by_c #( .w_in(wv), .c(r), .w_out(wv) ) mc( valns, vali[i+1] );

    // Update accumulated value.
    assign vali[i] = is_digit[i] ? valns + vald : 0;

    // Update number of digits.
    assign ndi[i] = !is_digit[i] ? 0 : is_digit[i+1] ? ndi[i+1] : i + 1;

  end

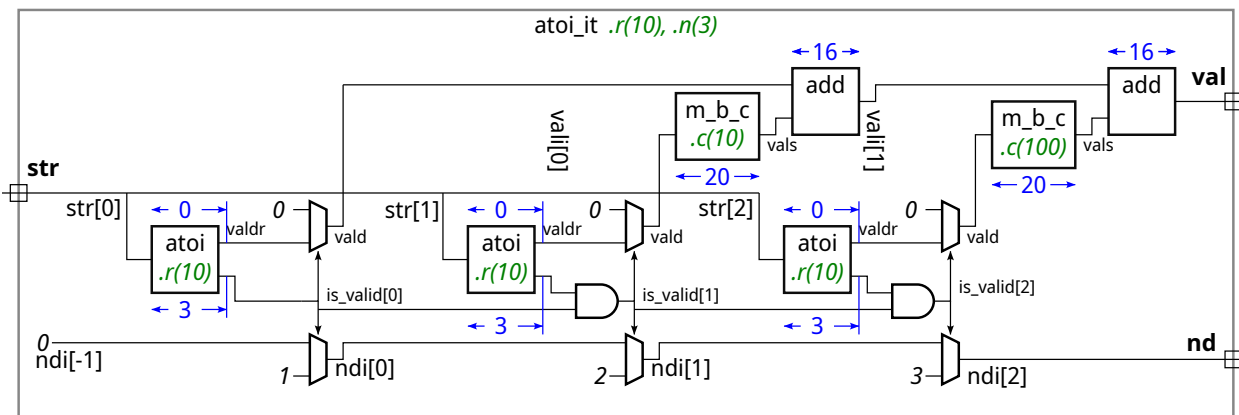
end
endmodule

```

Problem 3: [20 pts] Illustrated below is the hardware for one of the `atoi` modules from Homework 3. The delays for the `add`, `atoi1`, and `mult_by_c` modules are shown in blue. For `atoi` the delay of the value (`valdr`) output is zero and the delay of the `is_digit` (lower) output is 3.

(a) Based on the illustrated delays and using the simple model find the delay at each output, `val` and `nd`, and show the critical path to each.

- Use the simple model and indicated delays to find the delay at outputs `val` and `nd`.
- Show the critical path to both `val` and `nd`.
- Take into account constant values.



(b) Modify the design to reduce the delay at `val` by moving multiplexers. The modification is simple though will increase cost. Show your modification either on the diagram or in the Verilog code below.

- Modify to reduce the delay at `val` by moving multiplexers.
- Do not change what the module does.


```

module atoi_it
  #( int r = 11, n = 5, wv = $clog2( r**n ), wd = $clog2(n+1) )
  ( output logic [wv-1:0] val, output logic [wd-1:0] nd,
    input uwire [7:0] str [n-1:0] );

  uwire [wv-1:0] vali[n-1:-1];
  uwire is_valid[n-1:-1];
  uwire [wd-1:0] ndi[n-1:-1];
  assign is_valid[-1] = 1;
  assign ndi[-1] = 0;
  assign vali[-1] = 0;
  assign nd = ndi[n-1];
  assign val = vali[n-1];
  localparam int wcv = $clog2(r);

  for ( genvar i=0; i<n; i++ ) begin
    uwire [wcv-1:0] valdr;
    uwire is_digit;
    atoi1 #(r,wcv) a( valdr, is_digit, str[i] ); // Find Value of Digit i

    // Determine if this digit continues a sequence of valid digits.
    //
    assign is_valid[i] = is_digit && is_valid[i-1];

    // Replace value with zero if str[i] is not a digit, or if the
    // string of valid digits has already ended.
    //
    uwire [wcv-1:0] vald = is_valid[i] ? valdr : 0;

    // Multiply (scale) the digit value based on its position in the number.
    //
    uwire [wv-1:0] vals;
    mult_by_c #( .w_in(wcv), .c(r**i), .w_out(wv) ) mc( vals, vald );

    // Add the scaled digit to the value accumulated so far.
    //
    add #(wv) a1( vali[i], vali[i-1], vals );

    // Update the number of digits so far.
    //
    assign ndi[i] = is_valid[i] ? i+1 : ndi[i-1];

  end
endmodule

```

Problem 4: [12 pts] Answer each question below.

(a) The module below will not compile because of the way the module connections are declared. Fix the problem by changing the declarations.

- Change declaration to fix problem.

```
module yucx2
  #( int w = 5 )
  ( output uwire [w-1:0] x,
    input uwire [1:0] s,
    input uwire [w-1:0] a0, a1 );

  always_comb begin
    x = a0;
    if ( s != 0 ) x = a1;
  end
endmodule
```

(b) The mv output of findmax is supposed to be set to the value of the largest of the three inputs. Assuming it compiles and simulates, it still won't work. Identify the problem.

- Why won't mv be set to the maximum of a0, a1, a2?
- Provide an example that illustrates the incorrect behavior.

```
module findmax
  #( int w = 5 )
  ( output logic [w-1:0] mv,
    input uwire [w-1:0] a0, a1, a2 );

  initial mv = 0;
  always_comb if ( mv < a0 ) mv = a0;
  always_comb if ( mv < a1 ) mv = a1;
  always_comb if ( mv < a2 ) mv = a2;
endmodule
```

Problem 5: [12 pts] Answer each question below.

(a) Type `logic` is an example of a four-state type. Name those four states and describe what the non-numeric ones are used for.

- Name the four `logic` states.
- Describe what the non-numeric ones signify.

(b) Most synthesis programs will not synthesize a module that includes a delay, such as the one below. Why not?

```
module madd
  #( int w )
  ( output logic [w-1:0] w,
    input uwire [w-1:0] a, b, c );
  always_comb begin
    w = a * b;
    #5; // Allow enough time for multiplication to finish.
    w = w + a;
  end
endmodule
```

- Why isn't a delay synthesizable?