# Spring Simulation

Code in gpup/demo-2-springs.cc simulates of a string of beads.

Purpose is to demonstrate:

- Use of coordinate class pCoor and vector class pVect.
- Simulation of a spring.

Spring Simulation  $\gg$  Simulated World

### Simulated World

- *Point masses* connected by *ideal springs*.
- $\circ~$  First and last ball can be frozen in space.
- $\circ~$  Balls can collide with platform but not each other.
- Each ball has its own mass.
- $\circ~$  All springs are identical.

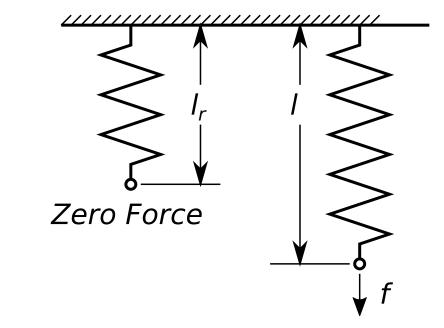
Spring Simulation  $\gg$  Hooke's Law

### Hooke's Law

Describes an ideal spring.

The magnitude of the force, f, is

 $f = h(l - l_r)$ 



where h is the spring constant,

where l is the current length of the spring,

 $l_r$  is the *relaxed* length of the spring.

# Computing force on ends of spring.

Consider a spring with one end at  $P_1$  and the other end at  $P_2$  ... ... with relaxed length  $l_r$  and spring constant h.

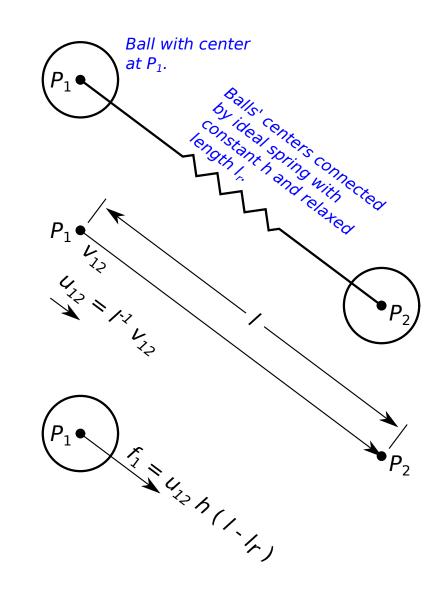
Let  $v_{12} = P_2 - P_1$ , the vector from  $P_1$  to  $P_2$ .

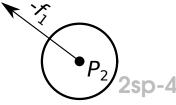
Let  $l = ||v_{12}||$ , the length of vector  $v_{12}$ .

Let  $u_{12} = \frac{1}{l}v_{12}$ , the unit vector pointing from  $P_1$  to  $P_2$ .

The force on  $P_1$  is  $f_1 = h(l - l_r)u_{12}$ .

The force on  $P_2$  is  $f_2 = -f_1 = h(l - l_r)u_{21}$ .





### Variables for Physical State

#### Ball class

No changes between demo-1-simple and demo-2-springs to the ball class were necessary to model the spring. But some members were added to make the simulation more interesting. The ball class in demo-1-simple had members only for position and velocity. Here we add members mass and radius so we can look at the effect of different masses.

#### Ball Array

Variable World::balls holds an array of Ball objects. This is allocated in the World::init function, and the ball objects are initialized in routines ball\_setup\_1, ball\_setup\_2, etc. (The different routines put the balls in different patterns, for example, ball\_setup\_2 forms them into a pendulum.)

# Spring modeling in demo-2-springs code

There is no special class used for springs. A spring is assumed between each pair of adjacent balls. (Adjacent based on the position in the **balls** array.) The length of the spring is just the distance between the respective balls. Each spring has a *relaxed length*, at which it gives no force (it will just stay at that length if no external forces act on it). Variable World::relaxed\_length is the relaxed length for all springs.

Variable World::opt\_spring\_constant holds the spring constant (h). To model spring friction two different spring constants are used. When a spring is being stretched (its length is larger than its relaxed length and getting larger) or compressed (its length is smaller than its relaxed length and getting smaller) spring constant World::opt\_spring\_constant is used to compute forces. When a spring is relaxing (its length is larger than its relaxed length but getting smaller, or its length is smaller than its relaxed length and getting larger) then World::opt\_spring\_constant \* 0.7 is used to compute forces.

### Coordinate and Vector Classes

The code uses a coordinate class pCoor and vector class pVect for the respective quantities. These classes are defined in file coord.h, and were written for this course. (There are many similar libraries one can use.)

File gpup/demo-0-coor.cc shows examples of how to use these.