# **Basic Setup**

Follow the instructions for class account setup on https://www.ece.lsu.edu/gp/proc.html. Code for this assignment is in directory ../hw/gpm/2023/hw02.

If the class account has been set up properly, the code can be built from within Emacs by pressing **F9** when visiting any file in the .../2023/hw02 directory or when in an Emacs shell buffer (which can be entered using **Alt**-x shell **Enter**). The code can be built from the command line using the command **make** -j 4 (assuming .../2023/hw02 is the current directory). Either method runs a makefile that builds all examples in the directory. It builds three versions of each program, one taking the base name of the main file, such as hw02, one with the suffix -debug, such as hw02-debug, and one with the suffix -cuda-debug, such as hw02-cuda-debug. The versions with the -cuda-debug suffix are compiled with host optimization turned off and CUDA debugging turned on, which facilitates debugging but slows down execution. To debug CUDA or host (CPU) code use the Cuda version of gdb, cuda-gdb. Note that the -cuda-debug versions will run much more slowly than the regular versions. The executables with the suffix -debug are compiled with host optimization turned off but CUDA debugging turned off. Use gdb or cuda-gdb to debug these.

Running make on a clean directory will produce a large amount of output. The make program and the file it reads, Makefile, are designed to build executables in a lazy fashion, meaning that they only create a file if it is not present or if its prerequisites have changed. Therefore a second run of make will take much less time.

Quickly check whether the build is successful with the command ./hw02. It should produce output ending with a line something like this 32 4.6 15 100 3 0.0 1014 1.0 4739 Ot 1978 +----.

The makefile will compile code for a GPU on the system it was run. Re-run make when moving to a different system. The Makefile should automatically detect whether the GPU for which the executable was built matches the GPU on the current system, and re-build if needed.

### **Background and Reference Material**

For this assignment one must be able to write, or at least modify, CUDA kernels. A good reference is the CUDA C++ Programming Guide, https://docs.nvidia.com/cuda/cuda-c-programming-guide/index.html. Focus on Chapter 5 up to and including 5.3 (Memory Hierarchy), but skip 5.2.1 (Thread Block Clusters). For sample code a good place to start is 2021 Homework 1, and other past assignments given in this course. The CUDA C used in this assignment is very close to C++20. A good reference for C and C++ is https://en.cppreference.com/w/.

In the references below some information is provided for specific architectures, either by CC (*e.g.*, 8.0) or by name (*e.g.*, Ampere). Both the CC 8.0 and CC 8.6 GPUs implement the Ampere architecture, 8.9 GPUs implement Ada Lovelace, and 9.0 implements Hopper. For this assignment only consider CC 8.x and 9.0 GPUs. The compute capability (CC) of the lab GPUs is shown on the system status page.

A solution to these problems requires some understanding of the hardware structure, in particular how requests are issued to the L1 cache. See Chapter 7 of the Programming Guide for the basics (but not including the L1 cache), and also Chapter 19 (Compute Capabilities) for some more details.

The hardware is covered in greater depth in the Kernel Profiling Guide,

https://docs.nvidia.com/nsight-compute/ProfilingGuide/index.html. Focus on Section 3.1 (Metrics Guide, Hardware Model) and Chapter 9 (Memory Chart). There is no need to read the material on *how* metrics are collected and there is no need to run the profiler yourself. The assignment code uses the CUPTI API to collect data. In class an MP (or SM) was described as having several-usually four-warp schedulers. The Profiling Guide refers to warp schedulers as sub partitions. For this assignment requests to the L1 cache are all global requests. Later in the semester we will make shared and maybe local requests, but probably not texture or surface requests.

### Using The Microbenchmarks

When tuning code it is important that one does not waste time trying to make the code go faster than what

the hardware can provide. *Microbenchmarks* can provide data on capabilities that will help one estimate hardware limits. In the course repo a set of microbenchmarks can be found in the cuda/microbenchmarks directory. They are compiled in the same way as other code samples. (Say, enter the command gmake.) A single executable, mb, is used for all of the microbenchmarks.

The mb program can run four microbenchmarks, atomic operations (a), MADD operation latency (o), memory latency  $(\mathbf{m})$ , and memory throughput  $(\mathbf{s})$ . The letters in parentheses indicate the command-line option to use to run the respective benchmark. For example, to run the memory latency benchmark invoke mb using the shell command ./mb m. Here is some output: [cyc2.ece.lsu.edu] % ./mb m GPU 0: NVIDIA GeForce RTX 4090 @ 2.52 GHz WITH 24214 MiB GLOBAL MEM GPU 0: L2: 73728 kiB MEM<->L2: 1008.1 GB/s GPU 0: CC: 8.9 SM: 128 SP-FP32/SM: 128 DP-FP64/SM: 2 TH/BL: 1024 GPU 0: SHARED: 49152 B/BL 102400 B/SM CONST: 65536 B # REGS: 65536 GPU 0: PEAK: 41288 SP GFLOPS 645 DP GFLOPS COMP/COMM: 163.8 SP 5.1 DP Using GPU 0 Global Load Latency Microbenchmark (Option 'm') CUDA Kernel Resource Usage: For mb\_g: 0 shared, 120 const, 0 loc, 26 regs; 1024 max threads per block. For mb\_ro: 0 shared, 120 const, 0 loc, 26 regs; 1024 max threads per block. Array size: 67108864 elts. Block size 32 thds. Kernel mb\_g: cyc !<---->! nbl iter Block Total ns 1024 20480 512 kiB 301 512 MiB 758 \*\*\*\*\*\*\*\*\*\*\*\*\*\* 1024 10240 256 kiB 256 MiB 303 763 \*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\* 252 512 10240 256 kiB 128 MiB 635 \*\*\*\*\*\*\*\*\*\*\*\*\* 256 10240 256 kiB 64 MiB 117 295 \*\*\*\*\*\* 128 10240 256 kiB 32 MiB 109 275 \*\*\*\*\*\* 64 10240 16 MiB 256 kiB 111 279 32 10240 256 kiB 8 MiB 111 279 \*\*\*\*\*\* 16 10240 4 MiB 256 kiB 114 287 8 10240 2 MiB 256 kiB 118 298 \*\*\*\*\*\* 10240 1 MiB 4 256 kiB 118 297 2 10240 256 kiB 512 kiB 129 324 \*\*\*\*\*\* 1 10240 256 kiB 256 kiB 129 324 \*\*\*\*\*\*\* 1 10000 128 kiB 128 kiB 125 315 \*\*\*\*\*\*\* 1 10000 64 kiB 64 kiB 20 51 \* 1 10000 32 kiB 32 kiB 17 44 \* 1 10000 16 kiB 16 kiB 16 40 \* 1 10000 8 kiB 8 kiB 15 38 \* 10000 15 37 \* 1 4 kiB 4 kiB 1 10000 2 kiB 2 kiB 15 37 \* 10000 1 1 kiB 1 kiB 14 36 \* 1 10000 512 В 512 В 14 36 \*

In this case, an exact latency is not provided. Instead memory latency is shown when accessing different amounts of memory. The values under the Block and Total columns indicate the amount of data accessed, and the values under the ns and cyc columns indicate the respective latency. Based on this data one can determine the sizes of the different cache levels, and their latencies. The L1 cache has a latency of about 38 cycles and appears to be between 64 and 128 kibibytes based on the microbenchmarks. (The API reports a

size of 102 kilobytes.) Similarly the L2 cache latency appears to be about 280 cycles and the size is between 64 and 128 mibibytes. Memory latency appears to be about 760 cycles.

The streaming microbenchmark shows the maximum throughput between various layers under different circumstances. It is selected with the **s** option: [cyc2.ece.lsu.edu] % ./mb s GPU 0: NVIDIA GeForce RTX 4090 @ 2.52 GHz WITH 24214 MiB GLOBAL MEM GPU 0: L2: 73728 kiB MEM<->L2: 1008.1 GB/s GPU 0: CC: 8.9 SM: 128 SP-FP32/SM: 128 DP-FP64/SM: 2 TH/BL: 1024 GPU 0: SHARED: 49152 B/BL 102400 B/SM CONST: 65536 B # REGS: 65536 GPU 0: PEAK: 41288 SP GFLOPS 645 DP GFLOPS COMP/COMM: 163.8 SP 5.1 DP Using GPU 0 Streaming Microbenchmark (Option 's') 49 Per Block 6272 kiB, 802816 kiB me\_n\_iter Per Kernel 12\_n\_iter 384 Per Block 49152 kiB, Per Kernel 55248 kiB 11\_n\_iter 800 Per Block 32 kiB, Per Kernel 4096 kiB --Insn----L1 Per SM--L2 GB/s-- DRAM \_\_\_ \_\_\_\_ GB/s Lv Blk V SPL s /add % SW TW BXW B/cyc /SM /GPU GB/s ME 128 1 2.5 2 7.5 s0 4 1 0.0 3.4 7.5 966 963 851 L2 128 1 38.2 4892 s0 1317 2.4 7 4 1 0.0 17.3 38.2 45 L1 128 2 s0 321 1.741 8 2 0.0 138.1 326.8 0.1 13 15 L1 128 1 s0 639 2.2 33 4 1 0.0 67.7 164.2 0.1 7 9 2.4 4 0.0 17.3 38.2 38.2 4892 43 L2 128 1 s0 1317 8 1 L2 64 1 2.4 4 0.0 31.9 74.3 74.3 4757 82 s0 677 8 1 L2 2 1 s0 621 2.4 0 4 1 0.0 32.6 81.0 81.0 162 81 L2 623 2.4 0 4 0.0 32.6 80.8 80.8 82 1 1 s0 1 81 L2 1 1 p1 622 2.4 0 4 2 0.0 32.6 80.9 80.9 81 81 L2 2.4 0 4 4 0.0 32.5 80.0 80.0 80 1 1 p2 629 80 L2 1 1 pЗ 746 2.4 0 8 8 0.0 27.4 67.5 70.1 70 68 L2 128 1 2.4 4 17.6 38.2 45 s0 1317 8 1 0.0 38.2 4893 L1 128 4 s0 320 1.4 34 16 4 0.0 147.3 327.4 13 13 0.1 L1 128 2 s0 320 1.7 41 8 2 0.0 139.0 328.1 0.1 13 15 L1 128 1 33 4 67.7 164.2 7 7 s0 639 2.2 1 0.0 0.1 7 7 L1 128 1 644 2.2 33 4 2 0.0 66.7 162.9 0.1 p1 L1 128 1 2.2 33 4 0.0 66.6 162.9 7 7 p2 644 4 0.1 2.2 33 8 0.0 7 L1 128 1 рЗ 640 8 67.1 163.9 0.1 8 L1 128 1 2.2 33 8 2 7 7 s1 641 1.0 67.1 163.7 0.1 L1 128 1 s2 2.2 17 16 4 3.0 34.7 82.5 0.0 3 3 1271 L1 128 1 s3 2552 2.2 8 32 8 7.0 17.1 41.1 0.0 2 2 L1 128 1 s4 5136 2.2 4 32 16 15.0 8.4 20.4 0.0 1 3 L1 128 1 s5 10372 2.2 2 32 32 31.0 4.1 10.1 0.0 0 1 Key SPL: Stride or Permute Pattern Lg s0, sequential pattern (stride 1) within warp. si, stride 2<sup>i</sup> within warp.

pi, Low five bits sequential, 2<sup>i</sup> distinct values for others.

Here is a brief description of the column headings. Lv indicates the memory hierarchy level being targeted: memory, L2 cache, or L1 cache.

Blk indicates how many blocks are participating. In most cases one would want one block per SM to participate. But for cases where, say, only one block at a time would be busy the rows with Blk equal 1 might be useful.

V indicates the vector length of the item accessed. A 1 is just an ordinary float, 2 is a two-element vector, and 4 is a four-element vector.

SPL describes the access pattern. A value of s0 is a simple sequential pattern where adjacent threads access adjacent elements. A value of si indicates that thread number  $\tau$  accesses element number  $\tau 2^i$ . So, s0is sequential, s1 is a stride of 2, etc. A stride of  $2^i$  for i > 0 will result in bank conflicts. A value starting with **p** is for a permutation pattern. Permutation patterns do not have bank conflicts (assuming element number x uses bank x mod 32), but within a warp there are  $2^i$  distinct values for bits 63:5 of the address for pattern pi. These patterns show how many tag lookups can be performed per warp without slowing things down. Based on the results above, up to four.

The /add column shows how many instructions were executed per arithmetic operation. The benchmark computes a sum using the loaded value. An ideal value is 1 + 1/v where v is the vector length.

The % column shows the instruction issue rate reported by Nvidia's CUPTI system. A value of 100% indicates that at each cycle an instruction could be issued by a warp scheduler. Based on the numbers above it looks like instructions requiring multiple cycles to dispatch, such as loads, make it impossible to reach 100%.

SW shows the number of sectors requested per warp for a memory instruction. Anything above 4 will likely result in reduced performance. TW shows the number of tag lookups per warp. (Caches manage data in units of *lines*. For each cached line a part of the data's address, called the *tag*, is stored. When a cache is checked for data the lookup address is compared to the tags of the cached data. A cache line in the Nvidia devices of at least CC 7 to 9 is 128 bytes, divided into four 32-byte sectors.) The value under BXW shows the number of bank conflicts per warp for a load instruction. Anything above 0 will result in reduced performance.

The B/cyc column shows the data throughput in bytes per SM per cycle. In recent Nvidia devices an SM has four warp schedulers with a warp size of 32, so that at best 128 threads per cycle can be issued. (In most cases one instruction.) So, a value of 128 in the B/cyc column means that each thread is getting one byte per cycle. In the microbenchmark threads are usually loading floats, which are 4 bytes. Also, in recent devices a load instruction takes four cycles to dispatch. So a value of 128 would indicate that loads are issuing without delay (beyond their four-cycle dispatch time). An H100, CC 9.0, actually attains about 128 bytes per cycle using scalar loads. This indicates that the scheduler can issue both a load instruction and an FP32 instruction in the same cycle. (Or it indicates this conclusion is wrong.) For the consumer-grade CC 8.9 device about half of this peak is attained for scalar loads. Note that for vector loads even a "cheap" RTX 4090 can execute at about 128 bytes per warp per cycle. That is likely due to the vector load requiring just four cycle to dispatch, but providing 2 or 4 floats. So, for a 2-element vector, dispatch time would be 4 + 1 = 5 cyc, while the time to read the data eight cycles based on 128 bytes per cycle. So for 2-element vectors instruction issue stalls waiting for the data.

The GB/s columns show the data throughput. The column under L1 Per SM shows the data throughput between the L1 cache and the SM registers. The values under the L2 columns show the throughput between the L1 and L2 caches. Those throughputs are shown per SM and for the entire GPU. Finally, the value under the DRAM column shows the throughput between the L2 cache and DRAM. In the row targeting memory, Lv=ME, the throughputs under each GB/s column should all be the same (after accounting for whether they are per SM or for the whole GPU). For the rows targeting the L2 cache, the throughput under the DRAM column should be much less than the others (ideally zero). For the rows targeting the L1 cache, the throughput under L2 should be much smaller than those under L1.

#### Using hw02

The code in hw02.cu contains several kernels that compute the output of part of a transformer neural network layer. The hw02 program takes one command-line argument, indicating how many blocks to launch. If the argument is zero or missing then the number of blocks will be set to the number of multiprocessors (which is the default). If the argument is negative then the number of blocks will be -aP, where a is the argument value and P is the number of MPs on the GPU.

#### **Computation Overview**

The code in the assignment package is based on the *transformer network* introduced by Vaswani *et al* [1]. The discussion in this section uses some of the notation from that paper. The code in this assignment computes the following matrix multiplication:

```
for ( int i_ws = 0; i_ws < d_ws; i_ws++ )
for ( int i_qkv = 0; i_qkv<d_qkv; i_qkv++ )
{
    acc_t q = 0;
    for ( int i_model = 0; i_model < d_model; i_model++ )
        q += w_qkv[ i_qkv * d_model + i_model ]
            * h_in[ i_ws * d_model + i_model ];
        h_qkv_cpu[ i_ws * d_qkv + i_qkv ] = q;
}</pre>
```

The input matrices are  $w_{qkv} \in \mathbb{R}^{d_{qkv} \times d_{model}}$  and  $h_{in} \in \mathbb{R}^{d_{model} \times d_{ws}}$ , and the output matrix is  $h_{qkv} \in \mathbb{R}^{d_{qkv} \times d_{ws}}$ , where  $d_{model}$ ,  $d_{qkv}$ , and  $d_{ws}$  are positive integers. The homework package performs the calculation at two different sizes, in the smaller one  $d_{model} = 32$ ,  $d_{qkv} = 96$ , and  $d_{ws} = 29700$ . With those sizes matrix  $w_{qkv}$  has 108 rows and 36 columns. Matrix  $h_{in}$  is much wider,  $36 \times 29700$ .

The data type for the inputs and outputs is acc\_t, and the data type for weights are wht\_t. Both of these are defined near the top of the file as float. In most DNN systems the weights would be defined as a 16-bit or sometimes even a smaller type.

```
The code above can be re-written:
```

```
for ( int i_sample = 0; i_sample < n_samples; i_sample++ )
for ( int i_word = 0; i_word < n_words; i_word++ )
for ( int i_qkv = 0; i_qkv<d_qkv; i_qkv++ )
{
    acc_t q = 0;
    for ( int i_model = 0; i_model < d_model; i_model++ )
        q += w_qkv[ i_qkv * d_model + i_model ]
           * h_in[ ( i_sample * n_words + i_word ) * d_model + i_model ];
        h_qkv_cpu[ ( i_sample * n_words + i_word ) * d_qkv + i_qkv ] = q;
}</pre>
```

by splitting the  $d_{ws}$  dimension into two,  $n_{samples}$  and  $n_{words}$ . The two code fragments are equivalent, the first is obviously simpler, the second reveals more detail about the  $h_{in}$  matrix. The two code fragments can read and write the same matrices. The solutions for this assignment can use either method of addressing the arrays.

## **Program Output**

Starting a run of hw02 ...

[koppel@grace hw02]\$ ./hw02

... produces the following output:

The first thing printed is information about each GPU connected to the system, followed by a line showing the chosen GPU:

```
GPU 0: NVIDIA GeForce RTX 4090 @ 2.52 GHz WITH 24214 MiB GLOBAL MEM
GPU 0: L2: 73728 kiB MEM<->L2: 1008.1 GB/s
GPU 0: CC: 8.9 SM: 128 SP-FP32/SM: 128 DP-FP64/SM: 2 TH/BL: 1024
GPU 0: SHARED: 49152 B/BL 102400 B/SM CONST: 65536 B # REGS: 65536
GPU 0: PEAK: 41288 SP GFLOPS 645 DP GFLOPS COMP/COMM: 163.8 SP 5.1 DP
Using GPU 0
```

This assignment will only work on GPUs of CC 8 or greater.

Most fields are self-explanatory. For example, L2 is the size of the level-2 cache and CC indicates that the device is of compute capability 8.9 (Ada). The MEM<->L2 field shows the off-chip bandwidth. SM indicates the number of streaming multiprocessors. CC/SM indicates the number of CUDA cores (single-precision functional units) per SM, DP/SM indicates the number of double-precision functional units per SM, and TH/BL is the maximum number of threads per block.

The amount of shared memory available is shown per block (B/BL) and per SM, this does not indicate whether any particular kernel is using that much shared memory or could use that much. The same line shows the amount of constant memory, and the number of registers available.

The next line, PEAK, shows FP operation bandwidth in which a fused multiply-add is counted as one operation. (Most of the rest of the world counts a multiply-add as two operations, but in this class it's one.) The COMP/COMM line gives the computation to communication ratio in floating-point operations per floating-point element transfers. (The information above was collected in part using the runtime library's cudaGetDeviceProperties function.)

Next, the program provides information on the network layers to be tested:

```
Layer shape 0: smpls=300. wds=99. heads=4. d_q=d_k=d_v=8.
Layer shape 0: d_qkv=96. d_model=32. d_ws=29700
Layer shape 0: w_qkv: 12 kiB h_in: 3712 kiB
Layer shape 1: smpls=30. wds=99. heads=8. d_q=d_k=d_v=64.
Layer shape 1: d_qkv=1536. d_model=512. d_ws=2970
Layer shape 1: w_qkv: 3072 kiB h_in: 5940 kiB
```

The layers used are specified in the constant array 1s near the top of hw02.cu.

When run without arguments or with a 0 as the first argument, such as ./hw02 0, the program launches each kernel multiple times, starting with 4 warps per block, up to 32 warps per block. For this assignment (hw 2) the number of warps per block will always be a power of 2. The number of blocks is set equal to the number of MPs. Run time and other information will be shown for each launch. If the argument -n then it will launch with n blocks per MP.

### **Performance Data**

Each kernel is run multiple times, starting with one warp per MP, in successive runs increasing the number of warps per MP. A line of performance data is printed for each run. The a portion of the output for an RTX 4090, showing unmodified kernel qkv\_base (and that kernel should not be modified) and kernel qkv\_base\_w2 with the assignment correctly solved.

```
Kernel (qkv_base<ls_d_model(layer_specs[0]),1,1,1>), using 39 regs
   ---Insn---- --L1--- -- L1<->L2 ---
wp /itr % TAc SW
                  BXW N-Rd N-Wr GB/s Imb
                                            t/s === Util: FP++ Insn-- =======
                          2
                                             108 +-----
 4
   3.6 17 100
                З
                   0.0
                             1.0
                                  173
                                       0t
                                  302
   3.6 30 100
                          2
                                       0t
                                              59 +-----
8
                3
                   0.0
                             1.0
16
   3.6 31 100
                3
                   0.0
                          2
                             1.0
                                  437
                                       0t
                                              40 ++-----
32
   3.7 31 100
                3
                   0.0
                          1
                             1.0
                                  460
                                       0t
                                              38 ++----
```

The output above shows the result one kernel, qkv\_base each run using layer 0. (The name shown is how the function was named, including the template parameter.) The number of registers used, 39, is also shown.

Column wp shows the number of warps per block in the run. If the number of blocks in a launch is not set to the number of MPs then there would be a column headed ac, which would show the number of resident warps per MP. (The number of resident warps per MP is a multiple of the number of warps per block. By default the number of blocks in a launch is set equal to the number of MPs, and in such a case the value in the ac column would match the wp column.)

The group of columns under the heading Insn show information about machine (SASS) instructions. The /iter column shows the measured number of machine instructions divided by the number the expected number of iterations of the d\_model loop:  $n_{\text{sample}}n_{\text{words}}d_{\text{qkv}}d_{\text{model}}$ . For the kernels in this assignment the number should be greater than 3 (two loads and a multiply/add), the closer to 3 the better. A higher number might indicate that the compiler is using more instructions than it needs to, perhaps because of the way the kernel was written. This might slow execution.

The TAc column shows workload balance within a block. A value of 100 is ideal. Lower numbers, such as 99p, are followed by a letter. The letter indicates the principal cause of the imbalance. A p indicates predicate-off instructions, and an d indicates warp divergence.

The warp scheduler is responsible for choosing a warp with an instruction ready to execute. Sometimes no such warp can be found. The two major reasons in this assignment are that each warp is waiting for an operand to arrive and that the memory system is busy and so memory instructions must be stalled. The number in the % column shows the percentage of time that a warp can be chosen. Let  $n_{\text{body}}$  denote the value in the /iter column and let  $\theta_{\text{I}}^{\%}$  denote the value in column %. In terms of these execution time is roughly proportional to  $100n_{\text{body}}/\theta_{\text{I}}^{\%}$ .

For the kernels in this assignment the value of /itr is low enough. If in your solution /itr is much larger, say 8.1, then you might try looking at your code. For the kernels initially provided with this assignment % will be less than 10. An ideal value is 100, but the best in the sample solution is 31.

The columns in the L1 group show how efficiently load instructions are issued to the L1 cache. These were discussed in a prior section. Briefly, SW shows the number of sectors requested per warp for a memory instruction. Anything above 4 will likely result in reduced performance. The value under BXW shows the number of bank conflicts per warp for a load instruction. Anything above 0 will result in reduced performance.

The columns in the L1<->L2 group show how much data is moving between the L1 and L2 caches. The N-Rd column (normalized amount of data read) shows how much data is read, scaled to the ideal amount. A value of 1 is ideal, and will be achieved if each element of the w\_qkv and h\_in arrays is read exactly once. A value of 2 indicates that on average each element was read twice. For qkv\_base the w\_qkv array is read by every block, and so it is read by every MP. Since for layer 0 w\_qkv, at 12 kiB, is smaller than the cache it is read just once per MP. Accounting only for w\_qkv the value of N-Rd would be the number of MPs. However, each element of h\_in is read by one or two MPs (you should be able to work out the reason for this on your own) and h\_in is much larger than w\_qkv in layer 0, so overall N-Rd is small, it would be just 1.367 with 128 MPs and assuming each element of h\_in were read once. In layer 1 w\_qkv is much larger, 3072 kiB, and could not fit in the L1 cache and so it must be re-read, inflating N-Rd.

The value under the N-Wr column (normalized amount of data written) shows how much data moved from L1 to L2, normalized to the ideal amount. It is much easier to achieve the ideal here.

The value under Imb shows workload imbalance. A 0 is ideal. A value of 10t indicates that execution is taking twice as long, 100% longer, based on time measurements. A value of 5i indicates that on block is using 50% more instructions than the average block.

The value under the GB/s shows the measured rate of data moving between the L1 and L2 caches (in either direction, but L2 to L1 dominates). The number includes all MPs. (A per MP number is a reasonable alternative but I can't keep changing my mind.) This will become a limiting factor for layer 1, but will not be a problem for layer 0.

The  $t/\mu s$  column shows the measured execution time in microseconds. To the right of  $t/\mu s$  is a bar graph showing how busy three resources are (based on certain assumptions). Three resources are tracked, FMA (fused multiply/add) instructions, shown with a +, FMA along with load instructions, shown with a -, and off-chip data transfer, shown with a \*. The right-most position of a resource's character indicates what fraction of the time that resource is busy. A resource is being used 100% of the time if its character reaches the rightmost position (the last = in the column heading over the bar graph).

That is true in the last line for the FMA resource, and in the penultimate line for the off-chip data transfer. In the last line we would say that the FP capability is being saturated (a good thing) and in the penultimate line we would say that data transfer is being saturated (also a good thing given the assumptions made). Those last two lines are fictional. Consider the line for the 16 warp per MP run. The – is a bit more than halfway to the end. That indicates that instruction throughput is more than half of the peak possible.

The FMA utilization is computed by assuming one multiply/add per loop iteration, or  $n_{\text{sample}}n_{\text{words}}d_{\text{qkv}}d_{\text{model}}$ FMAs. Then the amount of time it would take to issue that many FMAs is computed. That time is divided by the measured execution time to get the utilization. The amount of time to issue the FMAs is based on the GPU being used and should be accurate (up to CC 9.0).

The instruction utilization, -, includes the FMA plus two load instructions per FMA.

**Problem 1:** Modify  $qkv_hw2_a$  so that it improves instruction issue utilization by having one thread compute  $m_w \times m_h$  elements,  $m_h$  rows and  $m_w$  columns, of the output matrix,  $h_{qkv}$ . Doing so requires reading  $m_w d_{model}$  elements of  $h_{in}$  ( $m_w$  columns, each column having  $d_{model}$  rows) and  $m_h d_{model}$  elements of  $w_{qkv}$ , and then performing  $m_w m_h d_{model}$  multiply/add operations, thus reducing the dispatch time to  $[4/m_w + 4/m_h + 1]$  cyc for recent NVidia devices counting only load and multiply/add instructions. (Dispatch time would be [4 + 4 + 1] cyc if each thread computed one element of  $h_{qkv}$  per iteration.) Routine  $qkv_base$  computes  $m_w$  elements per iteration and has a dispatch time of  $[4/m_w + 4 + 1]$  cyc cycles.

Template parameter  $m_wd$  is already used for the number of columns of  $h_{qkv}$  to compute. Use template parameter  $m_ht$  for the number of rows of matrix  $h_{qkv}$  to compute. Template parameter  $m_dp$  will be used in the next problem. Assume that these template parameters will only be set to powers of two.

There are two main challenges in solving this problem correctly: distributing work evenly and avoiding bank conflicts. The impact of bank conflicts can be reduced in part by using vector load instructions (but those are optional).

**Problem 2:** Modify  $qkv_hw2_a$  or  $qkv_hw2_b$  so that it improves workload balance by using  $m_d$  threads to compute each element of  $h_{qkv}$ , where  $m_d$  is the value of template parameter  $m_dp$ . The default is  $m_dp=1$ , meaning that each element of  $h_{qkv}$  is computed by one thread. In fact, each thread is computing  $m_ht * m_wd$  elements, but that doesn't change the fact that each element is computed by one thread. Modify one (or both) of the routines so that each element is computed by  $m_d$  threads. To do so each thread executes a portion of the i\_model loop and then the resulting partial sum is added to the partial sum computed by the other threads computing the same element of  $h_qkv$ .

There are several ways to add together partial sums. Choose a method that is fastest. The easiest is to use an atomic add. Try using an atomic add initially, but then compare it to a technique using shared memory or warp shuffles.

### **References:**

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