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### Corrections: ROBUST and OPTIMAL CONTROL

Convention: Page  $xx$  is denoted as  $Pxx$ . Line  $xxx$  from the top of the page is denoted as  $Lxxx$  while line  $xx$  from the bottom of the page is denoted as  $-Lxx$ .

1. P5, -L9, “be covered in an one or two” should be “be covered in a one or two”
2. P7, -L2, “Note that” should be “Note while”
3. P37, L2,  $C_1 =$  and  $B_1 =$  should be  $C =$  and  $B =$ .
4. P75, -L6, “decreasingly order numbers” should be “decreasingly ordered numbers”
5. P80, L8, “maximally possible” should be “maximum possible”
6. P89, L3, “Then for any nonzero vector  $u_0 \in \mathbb{C}^m$  the output ...” should be “Then for any nonzero vector  $u_0 \in \mathbb{C}^m$  such that  $G(z_0)u_0 = 0$  the output ...”
7. P105-107, Table 4.1, second entry from the bottom, DELETE

$$\limsup_{t \rightarrow \infty} \|z(t)\| = \|G(j\omega_0)u_0\|$$

This is not correct. (Thanks to Prof. Richard Braatz for pointing out th error.)

Correspondingly delete lines 8 and 9 from the bottom of page 106.

Also the discussion on page 107 should be changed to:

It is interesting to see what this table signifies from the control point of view. To focus our discussion, let us assume that  $u(t) = u_0 \sin \omega_0 t$  is a disturbance or a command signal on a feedback system, and  $z(t)$  is the tracking error. Then we say that the system has good tracking behavior if  $z(t)$  is small in some sense, for instance,  $\limsup_{t \rightarrow \infty} \max_i |z_i(t)|$  is small. Note that

$$\limsup_{t \rightarrow \infty} \max_i |z_i(t)| = \|G(j\omega_0)u_0\|_\infty \quad (\text{induced matrix } \infty \text{ norm})$$

for any given  $\omega_0$  and  $u_0 \in \mathbb{R}^q$ . Now if we want to track signals from various channels, that is if  $u_0$  can be chosen to be any direction, then we would require that  $\|G(j\omega_0)\|_\infty$  be small. Furthermore, if, in addition, we want to track signals of many different frequencies, we then would require that  $\|G(j\omega_0)\|_\infty$  be small at all those frequencies. This interpretation enables us to consider the control system in the frequency domain even though the specifications are given in the time domain.

8. P114, -L9, “Hence the  $\infty$  of ..” should be “Hence the  $\infty$  norm of ..”
9. P119, L11,  $u = \frac{(s+2)}{3}(r - n - d) - \frac{s-1}{3}d$  should be  $u = \frac{(s+2)}{3}(r - n - d) + \frac{s-1}{3}d$ .
10. P124, Corollary 5.6, add the following at the end of corollary: “or equivalently,  $\det(I - P(s)\hat{K}(s))$  has no zeros in the closed right half plane.”

11. P124, -L6, -L5, and -L3, “number of open rhp poles” should be ”number of (closed) rhp poles”
12. P124, change Theorem 5.7 (ii) to “ $(I - P(s)\hat{K}(s))^{-1}$  is stable.” This correction does not affect any other results in the book.
13. P125, Theorem 5.8, a footnote on the Nyquist plot: the Nyquist contour is constructed so that all imaginary axis poles of  $P$  and  $K$  are counted as unstable ones.
14. P149, L11, “Theorem 6.3 holds” should be “Theorem 6.3 hold”
15. P152, -L7, “applies to multivariable system” should be “applies to multivariable systems”
16. P157, L5, “ $A_{11}$  is not asymptotically” should be “ $A_{11}$  is not asymptotically stable”
17. P159, -L6, “using the definition of  $B(s)$ ” should be “using the definition of  $\tilde{B}(s)$ ”
18. P162, Example can be simplified.

The above bound can be tight for some systems. For example, consider an  $n$ -th order transfer function

$$G(s) = \sum_{i=1}^n \frac{b_i}{s + a_i},$$

with  $a_i > 0$  and  $b_i > 0$ . Then  $\|G(s)\|_{\infty} = G(0) = \sum_{i=1}^n b_i/a_i$  and  $G(s)$  has the following state space realization

$$G = \left[ \begin{array}{ccc|c} -a_1 & & & \sqrt{b_1} \\ & -a_2 & & \sqrt{b_2} \\ & & \ddots & \vdots \\ & & & -a_n \\ \hline \sqrt{b_1} & \sqrt{b_2} & \cdots & \sqrt{b_n} \\ & & & 0 \end{array} \right]$$

and the controllability and observability Gramians of the realization are given by

$$P = Q = \left[ \frac{\sqrt{b_i b_j}}{a_i + a_j} \right].$$

It is easy to see that  $\sigma_i = \lambda_i(P) = \lambda_i(Q)$  and

$$\sum_{i=1}^n \sigma_i = \sum_{i=1}^n \lambda_i(P) = \text{trace}(P) = \sum_{i=1}^n \frac{b_i}{2a_i} = \frac{1}{2} G(0) = \frac{1}{2} \|G\|_{\infty}.$$

In particular, let  $a_i = b_i = \alpha^{2i}$ , then  $P = Q \rightarrow \frac{1}{2} I_n$ , i.e.,  $\sigma_j \rightarrow \frac{1}{2}$  as  $\alpha \rightarrow \infty$ .

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19. P218, -L7, delete “and  $\|M\|_\infty = \bar{\sigma}(M(j\omega_0)) = \sigma_1$ .”
20. P222, -L17, “ $\det(I + W_1\Delta W_2KS_0) = \det(I + S_0W_1\Delta W_2K)$ ” should be “ $\det(I + W_1\Delta W_2KS_0) = \det(I + S_0W_1\Delta W_2K)$ ”
21. P248, L5, “ $\triangleq$ ” should be “:=” for consistence.
22. P248, -L8,  $u = \Delta_u y_2$  should be  $u_2 = \Delta_u y_2$ .
23. P258, L2, “ $N = \begin{bmatrix} I & \sqrt{2}I \\ -\sqrt{2}I & -I \end{bmatrix}$ ” should be “ $N = \begin{bmatrix} -I & -\sqrt{2}I \\ \sqrt{2}I & I \end{bmatrix}$ ”
24. P280, L13, “in simple cases” should be “in these simple cases”
25. P363, L7, L8, L12,  $B_1^*X + D_1^*C_1$  should be  $B_1^*X_1 + D_1^*C_1$ .
26. P457 -L8, “ $\Phi = 0$ ” should be “ $Q = 0$ ”
27. P488, -L1,  $[W_1 PW_2^{-1}]$  should be  $[W_1 KW_2^{-1}]$
28. P489, Figure 18.5,  $W_2$  and  $W_2^{-1}$  should be swapped.
29. P490, equation (18.7) should be  $(K_\infty^{-*}K_\infty^{-1} + I) \leq \gamma^2(K_\infty^{-*} + P_s^*)\tilde{M}_s^*\tilde{M}_s(K_\infty^{-1} + P_s)$ .
30. P492, Theorem 8.10,  $\underline{\sigma}(K_\infty)$  should be “ $\bar{\sigma}(K_\infty)$ ”, two times.
31. P494, L10,

$$\bar{\sigma}(\tilde{M}_s) = \bar{\sigma}(M_s) = \left( \frac{1}{1 + \bar{\sigma}^2(W_2PW_1)} \right)^{1/2}$$

should be

$$\bar{\sigma}(\tilde{M}_s) = \bar{\sigma}(M_s) = \left( \frac{1}{1 + \underline{\sigma}^2(W_2PW_1)} \right)^{1/2}$$

32. P494, L8 and L9

$$\bar{\sigma}^2(\tilde{M}_s) = \lambda_{max}(\tilde{M}_s^*\tilde{M}_s) = \frac{1}{1 + \lambda_{max}(P_sP_s^*)} = \frac{1}{1 + \bar{\sigma}^2(P_s)}$$

should be

$$\bar{\sigma}^2(\tilde{M}_s) = \lambda_{max}(\tilde{M}_s^*\tilde{M}_s) = \frac{1}{1 + \lambda_{min}(P_sP_s^*)} = \frac{1}{1 + \underline{\sigma}^2(P_s)}$$

and

$$\bar{\sigma}^2(\tilde{N}_s) = 1 - \bar{\sigma}^2(\tilde{M}_s) = \frac{\bar{\sigma}^2(P_s)}{1 + \bar{\sigma}^2(P_s)}$$

should be

$$\bar{\sigma}^2(\tilde{N}_s) = 1 - \underline{\sigma}^2(\tilde{M}_s) = \frac{\bar{\sigma}^2(P_s)}{1 + \bar{\sigma}^2(P_s)}$$

33. P587, reference no. 214, add “pp. 5-16” at the end.