Outline

MIPS Pipelined Implementations

Outline

Unpipelined Implementation. (Diagram only.)

Pipelined MIPS Implementations: Hardware, notation, hazards.

Dependency Definitions.

Data Hazards: Definitions, stalling, bypassing.

Control Hazards: Squashing, one-cycle implementation.

Outline: (Covered in class but not yet in set.)

Operation of nonpipelined implementation, elegance and power of pipelined implementation. (See text.)

Computation of CPI for program executing a loop.

Practice Problems

Practice Problems

The problems below provide practice for the material covered in this set.

Easier Branch Hardware Problems

2015 Homework 2 Problem 3 — Control logic for IF-stage PC mux.

2016 Homework 2 Problems 1,2 — Taken signal for a bltz, and bypass hardware and control.

Easier Non-Branch Hardware

2012 Midterm Problem 1 — PED and logic to generate stalls due to missing bypasses.

Slightly More Difficult Branch Problems

2019 Midterm Problem 3 — Avoid stall for slt/bne dependences.

2018 Homework 3 Problem 2 — Modify hardware (incl PC mux logic) so that bgt is resolved in EX

2017 Homework 3 Problem 1 — Implement bgezall (annulled and link)

Practice Problems

2015 Homework 2 Problem 2 — New MIPS bfeq. Reg fields are two bits each.

Slightly More Difficult Non-Branch Problems

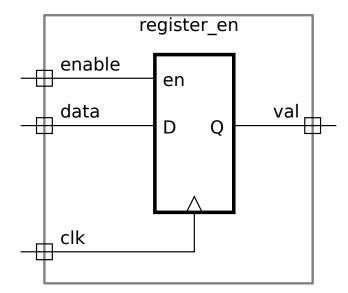
2020 Homework 2 — An integer multiplier with quicker results for special cases.

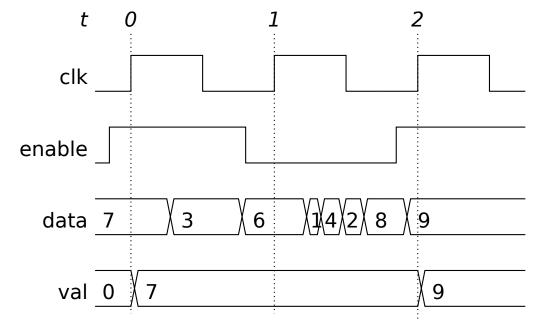
2017 Homework 5 Problem 3 — Bypass paths that can only accommodate 12 bits.

Some Components \gg Edge-Triggered Register

Some Components

Edge-Triggered Register



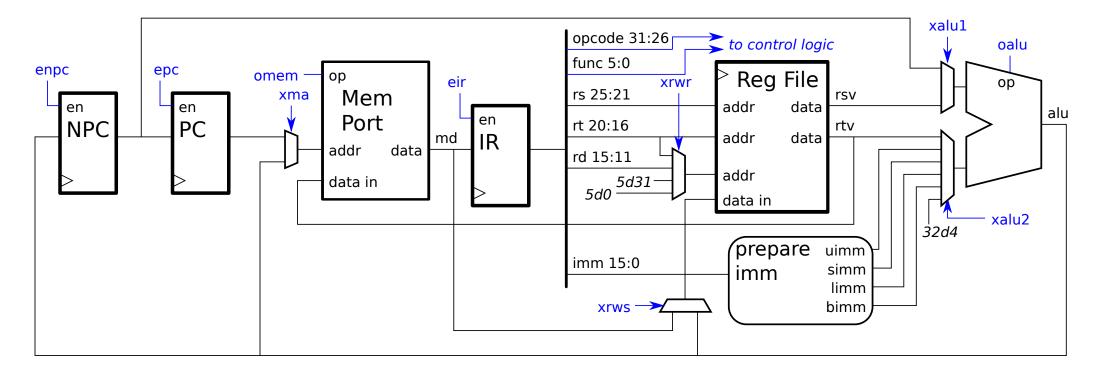


Very Simple MIPS Implementations >> Minimum Hardware Multi-cycle Implementation

Very Simple MIPS Implementations

Minimum Hardware Multi-cycle Implementation

From EE 3755 (as offered by dmk).

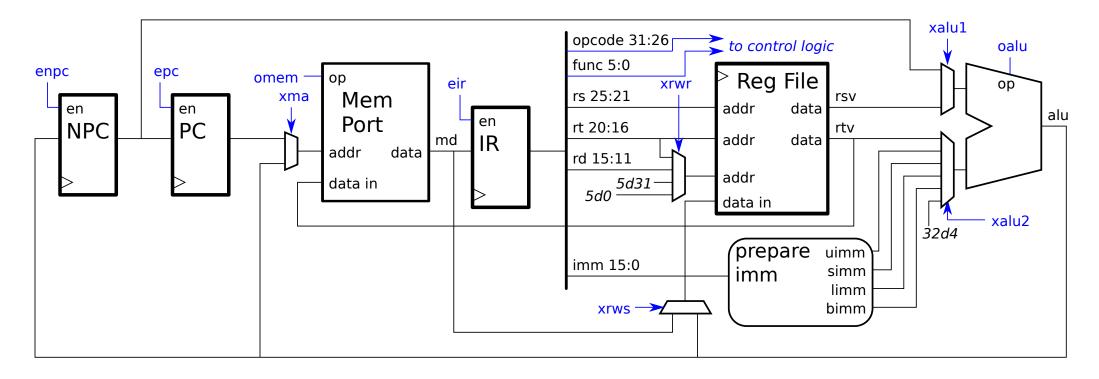


Very Simple MIPS Implementations >> Minimum Hardware Multi-cycle Implementation

Features

Avoid duplication of hardware: One Memory Port, One Adder (ALU).

Relatively complex control logic needed to re-use ALU, etc.



Unpipelined Implementation

In this implementation hardware is duplicated.

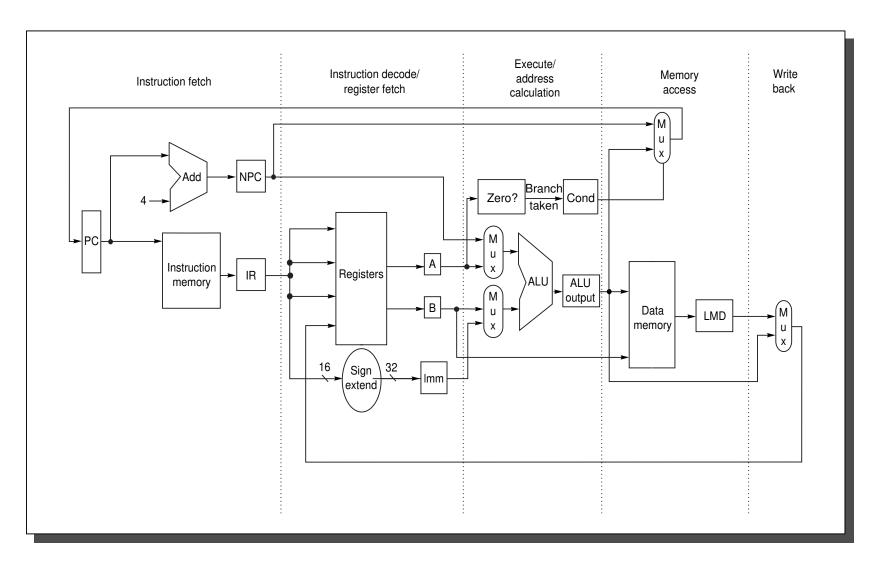
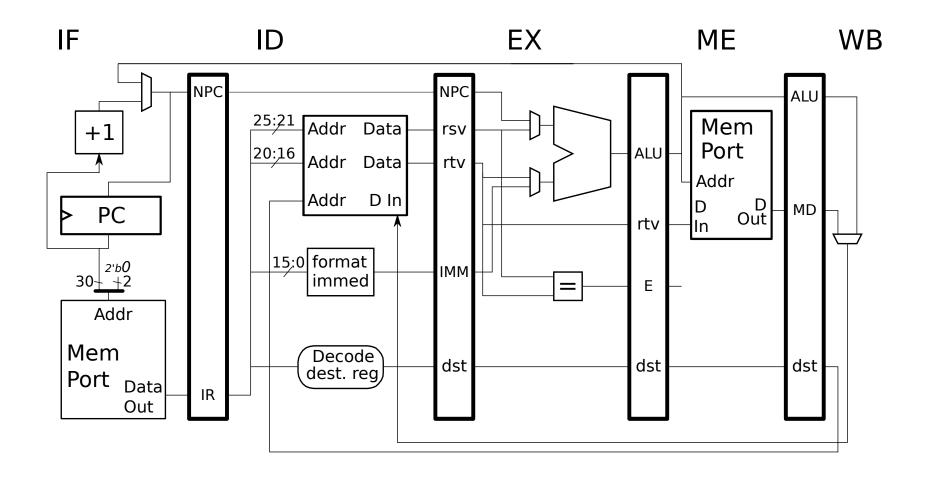


FIGURE 3.1 The implementation of the DLX datapath allows every instruction to be executed in four or five clock cycles.

Pipelining Terminology and Concepts \gg Pipelined MIPS Implementation

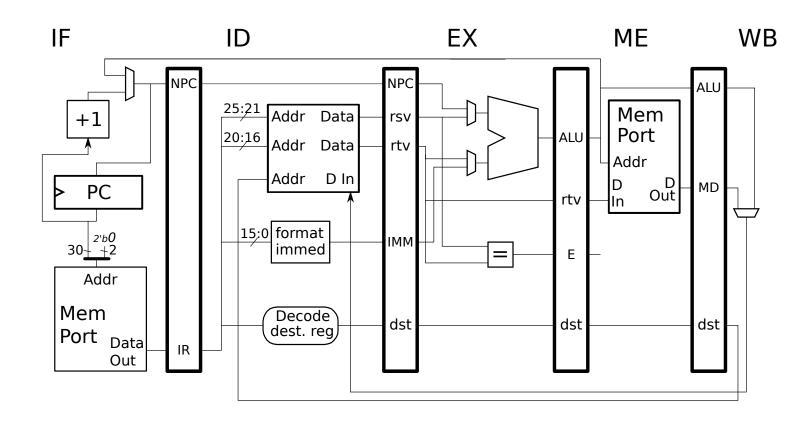
Pipelining Terminology and Concepts

Pipelined MIPS Implementation



Pipelining Idea

```
Split hardware into n equally sized (in time) stages ... ... separate the stages using special registers called pipeline latches ... ... increase the clock frequency by \lesssim n \times \ldots ... avoid problems due to overlapping of execution.
```



Pipelining Terminology and Concepts ≫ Pipeline Stages and Latches ≫ Stages

Pipeline Stages and Latches

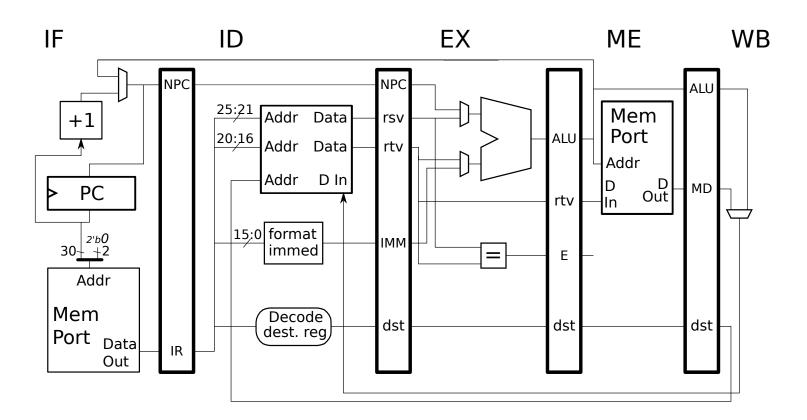
Pipeline divided into stages.

Each stage occupied by at most one instruction.

At any time, each stage can be occupied by its own instruction.

Stages given names: IF, ID, EX, ME, WB

Sometimes ME written as MEM.



Pipelining Terminology and Concepts \gg Pipeline Stages and Latches \gg Latches

Pipeline Latches:

Registers separating pipeline stages.

Written at end of each cycle.

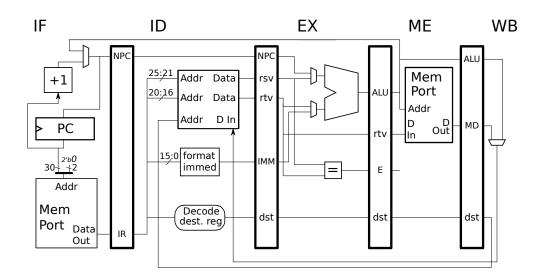
To emphasize role shown in diagram as bar separating stages.

Registers named using pair of stage names and register name.

For example, IF/ID.IR, ID/EX.dst, ID/EX.rsv (used in text, notes).

For brevity first stage name dropped: ID.IR, EX.dst, EX.rsv.

if_id_ir, id_ex_ir, id_ex_rs_val (used in Verilog code).



Pipelining Terminology and Concepts ≫ Pipeline Execution Diagram

Pipeline Execution Diagram

Pipeline Execution Diagram:

Diagram showing the pipeline stages that instructions occupy as they execute.

Time on horizontal axis, instructions on vertical axis.

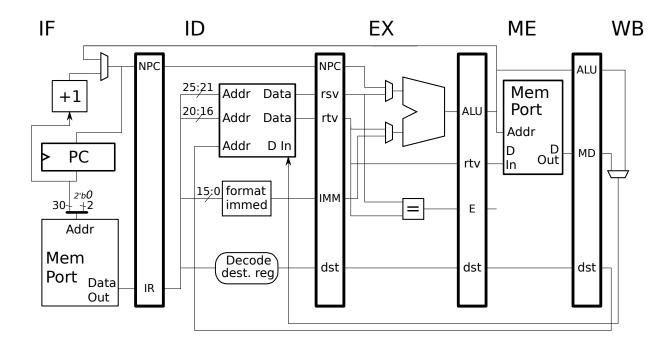
Diagram shows where instruction is at a particular time.

```
# Cycle 0 1 2 3 4 5 6
add r1, r2, r3 IF ID EX ME WB
and r4, r5, r6 IF ID EX ME WB
lw r7, 8(r9) IF ID EX ME WB
```

A vertical slice (e.g., at cycle 3) shows processor activity at that time.

In such a slice a stage should appear at most once ...

- ... if it appears more than once execution not correct ...
- ... since a stage can only execute one instruction at a time.



Instruction Decoding and Pipeline Control

Pipeline Control:

Setting control inputs to devices including ...

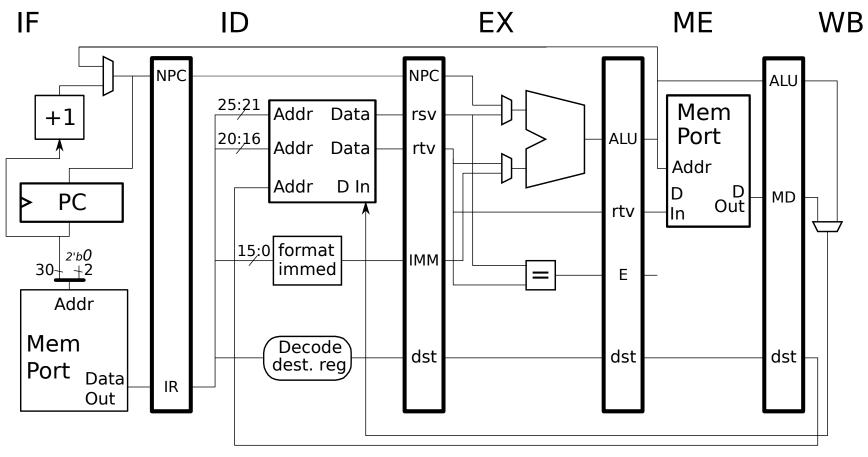
... multiplexor inputs ...

... function for ALU ...

... operation for memory ...

... whether to clock each register ...

... et cetera.



Pipelining Terminology and Concepts >> Instruction Decoding and Pipeline Control

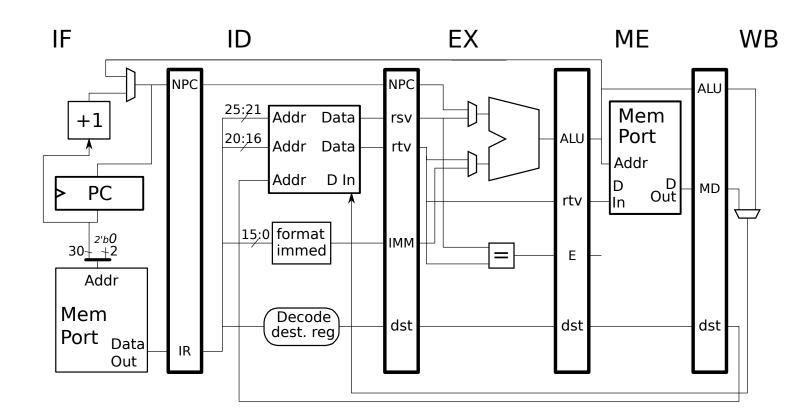
Options for controlling pipeline:

- Decode in ID

 Determine settings in ID, pass settings along in pipeline latches.
- Decode in Each Stage
 Pass opcode portions of instruction along.
 Decoding performed as needed.

Many systems decode in ID.

Example given later in this set.



Dependencies and Hazards

Dependencies and Hazards

Remember that sources **read from** registers in ID and results **written to** registers in WB.

Consider the following **incorrect execution**:

```
# Cycle
                                  5
                                         7
                          3
                                     6
add R1, r2, r3 IF ID EX
                          ME
sub R4, R1, r5 IF ID
                          EX ME
and r6, R1, r8
                      IF
                          ID
                                     WB
xor r9, R4, r11
                          IF
                              ID
                                 ΕX
                                     \texttt{ME}
                                         WB
```

Execution incorrect because ...

```
... sub reads r1 before add writes (or even finishes computing) r1, ... and reads r1 before add writes r1, and ...
... xor reads r4 before sub writes r4.
```

```
# Cycle
                                  3
add R1, r2, r3 IF
                             EX
sub R4, R1, r5
                                  ΕX
                        \mathsf{IF}
                             ID
                                      \texttt{ME}
                                           WB
and r6, R1, r8
                             IF
                                  ID
                                      EX
                                                WB
xor r9, R4, r11
                                  IF
                                           EX
                                                \mathtt{ME}
                                                     WB
```

Incorrect execution due to...

... dependencies in program...

... and hazards in hardware (pipeline).

Incorrect execution above is the "fault" of the hardware...

... because the ISA does not forbid dependencies.

Dependencies and Hazards \gg Distinguishing Definitions

Distinguishing Definitions

Dependency:

A relationship between two instructions ...

... indicating that their execution should be (or appear to be) in program order.

Hazard:

A potential execution problem in an implementation due to overlapping instruction execution.

There are several kinds of dependencies and hazards.

For each kind of dependence there is a corresponding kind of hazard.

Dependencies and Hazards ≫ Dependencies

Dependencies

Dependency:

A relationship between two instructions . . .

... indicating that their execution should be, or appear to be, in program order.

If B is dependent on A then B should appear to execute after A.

Dependency Types:

- True, Data, or Flow Dependence (Three different terms used for the same concept.)
- Anti Dependence
- Output Dependence
- Control Dependence

Anti- and Output-Dependencies are both Name Dependencies.

Data Dependence

```
Data Dependence: (a.k.a., True and Flow Dependence)
A dependence between two instructions . . .
. . . indicating data needed by the second is produced by the first.
```

Example:

```
add R1, r2, r3
sub R4, R1, r5
and r6, R4, r7
```

```
The sub is dependent on add (via r1).
```

The and is dependent on sub (via r4).

The and is dependent add (via sub).

Execution may be incorrect if ...

```
... a program having a data dependence ...
```

... is run on a processor having an uncorrected RAW hazard.

Dependencies and Hazards \gg Dependencies \gg Anti Dependence

Anti Dependence

Anti Dependence:

```
A dependence between two instructions ...
```

... indicating a value written by the second ...

... that the first instruction reads.

Antidependence Example

```
add r1, R2, r3 sub R2, r4, r5
```

sub is antidependent on the add.

Execution may be incorrect if ...

... a program having an antidependence ...

... is run on a processor having an uncorrected WAR hazard.

Dependencies and Hazards » Dependencies » Output Dependence

Output Dependence

Output Dependence:

```
A dependence between two instructions ...
... indicating that both instructions write the same location ...
... (register or memory address).
```

Output Dependence Example

```
add R1, r2, r3
sub R1, r4, r5
```

The sub is output dependent on add.

Execution may be incorrect if ...
... a program having an output dependence ...
... is run on a processor having an uncorrected WAW hazard.

Control Dependence

Control Dependence:

```
A dependence between a branch instruction and a second instruction ... ... indicating that whether the second instruction executes ... ... depends on the outcome of the branch.
```

```
beq $1, $0 SKIP  # Recall that branch has a delay slot.
nop
add $2, $3, $4
SKIP:
sub $5, $6, $7
```

The add is control dependent on the beq.

The sub is not control dependent on the beq.

Dependencies and Hazards \gg Pipeline Hazards \gg Types of Hazards

Pipeline Hazards

Hazard:

A potential execution problem in an implementation due to overlapping instruction execution.

Interlock:

Hardware that avoids hazards by stalling certain instructions when necessary.

Hazard Types:

Structural Hazard:

Needed resource currently busy.

Data Hazard:

Needed value not yet available or overwritten.

Control Hazard:

Needed instruction not yet available or wrong instruction executing.

Dependencies and Hazards \gg Pipeline Hazards \gg Data Hazards \gg Types of Data Hazards

Data Hazards

Identified by acronym indicating correct operation.

- RAW: Read after write, akin to data dependency.
- WAR: Write after read, akin to anti dependency.
- WAW: Write after write, akin to output dependency.

MIPS implementations above only subject to RAW hazards.

RAR not a hazard since read order irrelevant (without an intervening write).

Dependencies and Hazards \gg Pipeline Hazards \gg Data Hazards \gg Stalls

Stalls

When threatened by a hazard:

• Stall (Pause a part of the pipeline.)

Stalling avoids overlap that would cause error.

This does slow things down.

• Add hardware to avoid the hazards.

Details of hardware depend on hazard and pipeline.

Several will be covered.

Dependencies and Hazards \gg Pipeline Hazards \gg Structural Hazards

Structural Hazards

Cause: two instructions simultaneously need one resource.

Solutions:

Stall.

Duplicate resource.

Pipelines in this section do not have structural hazards.

Covered in more detail with floating-point instructions.

Avoiding Data Hazards

Avoiding Data Hazards

Pipelined MIPS Subject to RAW Hazards.

Consider the following **incorrect execution** of code containing data dependencies.

```
# Cycle
                            3
add R1, r2, r3 IF ID EX
                            ME
sub R4, R1, r5 IF ID
                            EX ME
and r6, R1, r8
                        IF
                            ID
                                       WB
xor r9, R4, r11
                            IF
                                ID
                                   ΕX
                                       \texttt{ME}
                                           WB
```

Execution incorrect because ...

```
... sub reads r1 before add writes (or even finishes computing) r1, ... and reads r1 before add writes r1, and ...
... xor reads r4 before sub writes r4.
```

Problem fixed by *stalling* the pipeline.

Avoiding Data Hazards >> Stalling

Stall:

To pause execution in a pipeline from IF up to a certain stage.

With stalls, code can execute correctly:

For code on previous slide, stall until data in register.

```
# Cycle
                                                    9
                                                        10
add R1, r2, r3 IF ID EX
                            {\sf ME}
sub R4, R1, r5
                                    ΕX
and r6, R1, r8
                                    ID EX
                        IF
                                                WB
xor r9, R4, r11
                                    IF
                                        ID
                                                EX ME
                                                       WB
```

Arrow shows that instructions stalled.

Stall creates a bubble, stages without valid instructions, in the pipeline.

With bubbles present, CPI is greater than its ideal value of 1.

Stall Implementation

Stall implemented by asserting a *hold* signal . . .

- ... which inserts a nop (or equivalent) after the stalling instruction ...
- ... and disables clocking of pipeline latches before the stalling instruction.

```
# Cycle
                                                                  10
                                                             9
add R1, r2, r3 IF ID EX
                                 \mathtt{ME}
sub R4, R1, r5
                                                    WB
and r6, R1, r8
                             IF
                                          ID
                                              EX
                                                        WB
xor r9, R4, r11
                                               ID
                                                        \mathsf{EX}
                                                             {	t ME}
                                                                 WB
```

During cycle 3, a nop is in EX.

During cycle 4, a nop is in EX and ME.

The two adjacent nops are called a bubble

... they move through the pipeline with the other instructions.

A third nop is in EX in cycle 7.

Avoiding Data Hazards ≫ Bypassing

Bypassing

Some stalls are avoidable.

Consider again:

```
# Cycle
                                      5
                                                          10
                             3
                                                      9
add R1, r2, r3 IF
                             ME
                     ID
                         ΕX
sub R4, R1, r5
                IF
                         ID
                             EX
                                 ME
                                      WB
and r6, R1, r8
                         IF
                             ID
                                 EX
                                      ME
                                          WB
xor r9, R4, r11
                                     EX
                              IF
                                  ID
                                         \texttt{ME}
                                              WB
```

Note that the new value of r1 needed by sub ...

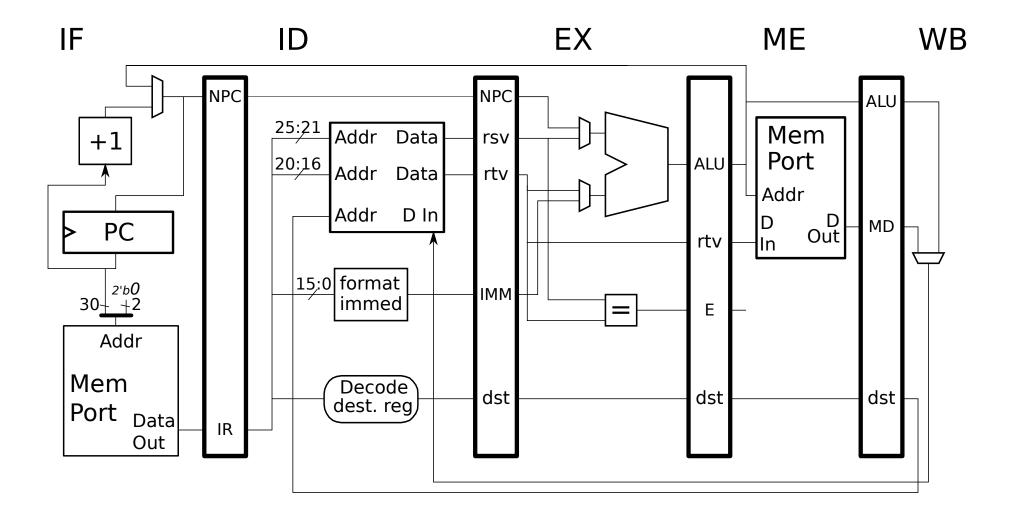
- ... has been computed at the end of cycle 2 ...
- ... and isn't really needed until the beginning of the next cycle, 3.

Execution was incorrect because the value had to go around the pipeline to ID.

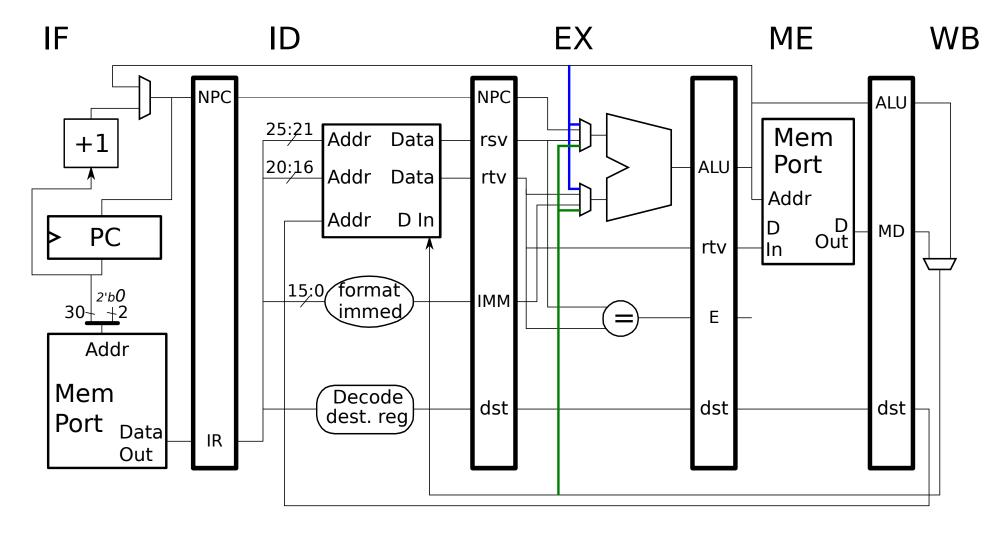
Why not provide a shortcut?

Why not call a shortcut a bypass or forwarding path?

Non-Bypassed MIPS



Bypassed MIPS



MIPS Implementation With Some Bypass Paths

```
# Cycle 0 1 2 3 4 5 6 7

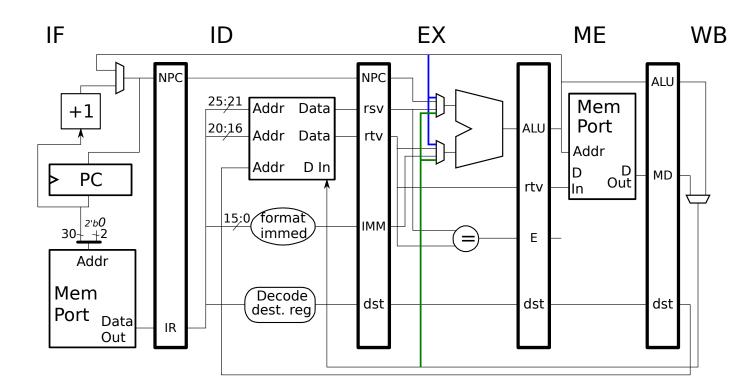
add R1, r2, r3 IF ID EX ME WB

sub R4, R1, r5 IF ID EX ME WB

and r6, R1, r8 IF ID EX ME WB

xor r9, R4, r11 IF ID EX ME WB
```

It works!



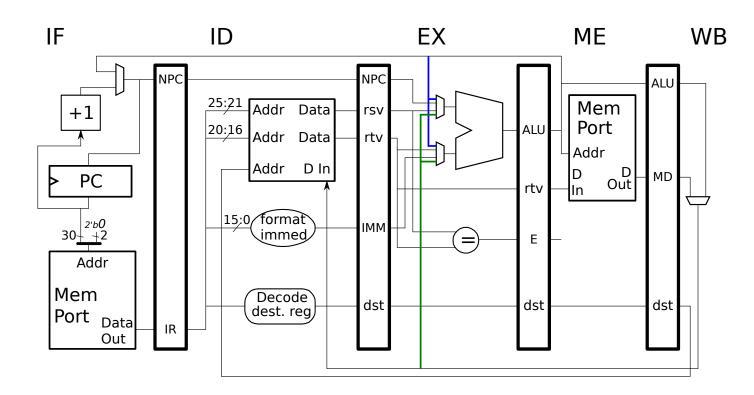
Avoiding Data Hazards \gg Bypassing \gg Unbypassable Hazards

Some stalls unavoidable.

```
# Cycle 0 1 2 3 4 5 6 7 8 9 10 lw R1, O(r2) IF ID EX ME WB add R1, R1, r4 IF ID -> EX ME WB sw 4(r2), R1 IF -> ID ----> EX ME WB addi r2, r2, 8
```

Stall due to lw could not be avoided with a bypass path (data not available in cycle 3).

Stall in cycles 5 and 6 could be avoided with a new bypass path.

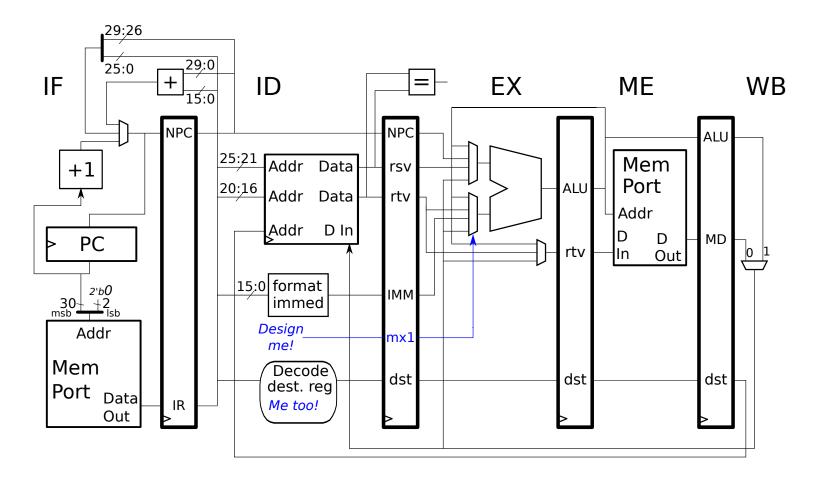


Control Logic Design Example(s)

Control Logic Design Example(s)

In this part design logic to determine dst ...

... and using that the bypass control logic for lower ALU mux.



Control Logic Design Example(s) > Logic to Determine Dst

Logic to determine dst for register file.

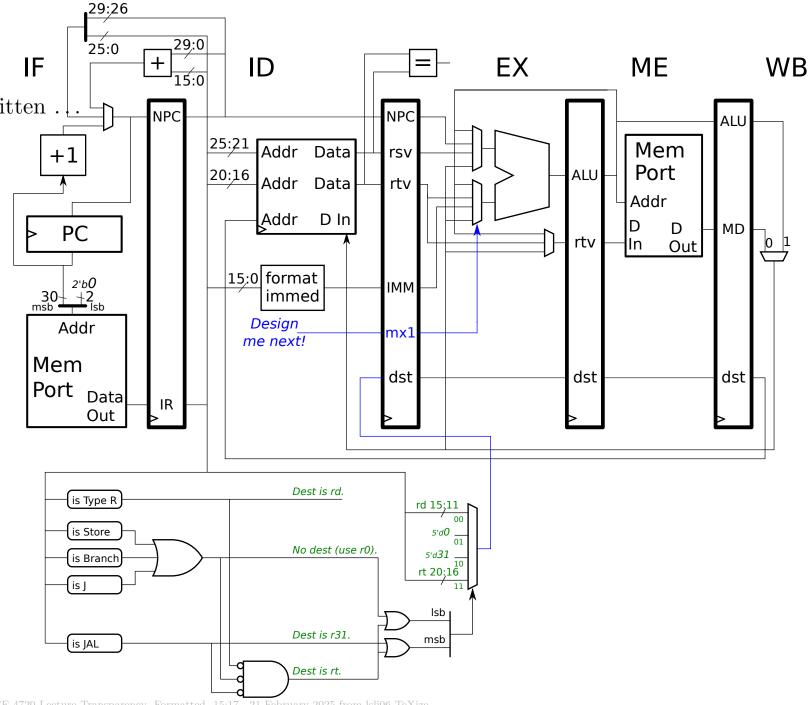
Note: dst is the register that will be written .

... or 0 if no register is written.

Depending on the instruction ...

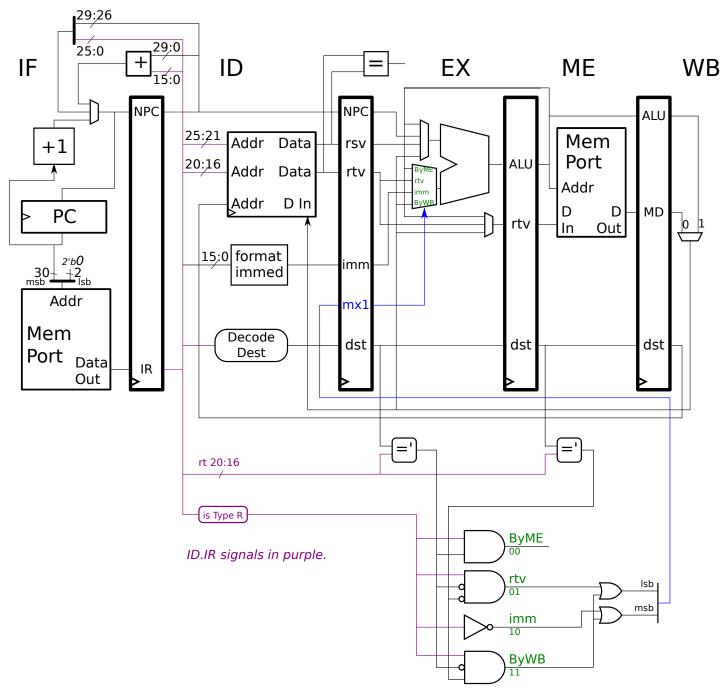
... the value is in the rd or rt field ...

 \dots or is the constant 0 or 31.



Control Logic Design Example(s) >> Bypass Control Logic for Lower ALU Mux

Bypass Control Logic for Lower ALU Mux



Control Logic Design Example(s) >> Bypass Control Logic for Lower ALU Mux

Notes about logic:

Control logic not minimized (for clarity).

Control Logic Generating dst.

Present in previous implementations, just not shown.

Determines which register gets written based on instruction.

Instruction categories used in boxes such as = is Store (some instructions omitted):

- = is Type R: All Type R instructions.
- = is Store : All store instructions.
- = is Branch: branches such as beq and bltz.
- = is JAL, = is J: Matches the exact instruction.

Control Logic Design Example(s) >> Bypass Control Logic for Lower ALU Mux

Logic Generating ID/EX.MUX.

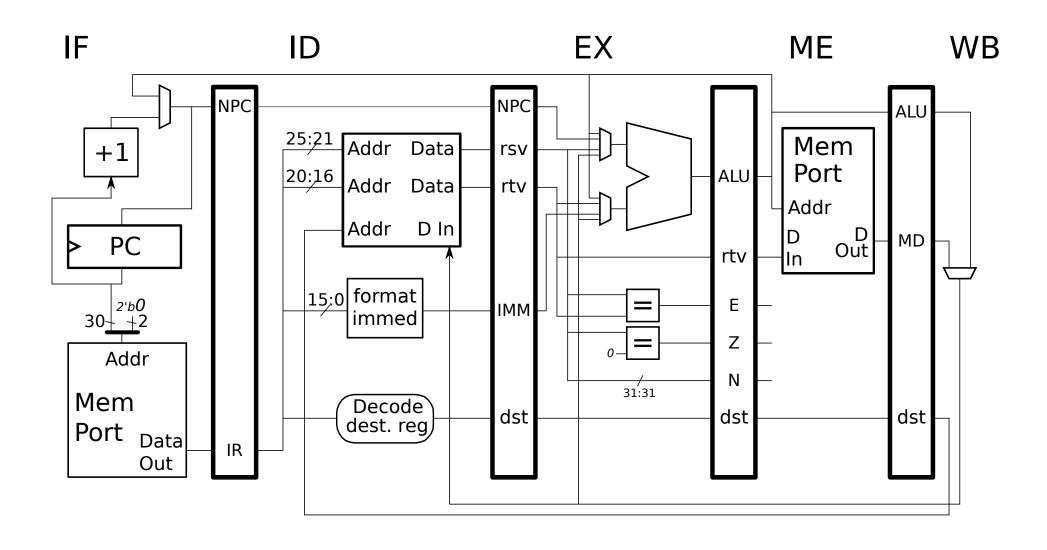
=' box determines if two register numbers are equal.

Register number zero is not equal register zero, nor any other register.

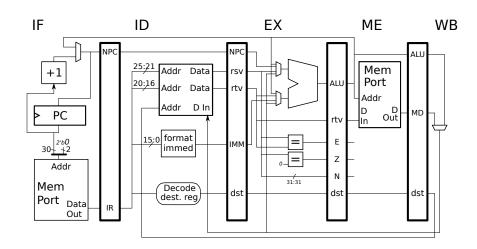
(The bypassed zero value might not be zero.)

Branch Hardware

Consider:



Branch Hardware ≫ Branch Execution



Example of incorrect execution

```
#I Adr
               Cycle
                                                        8
      bgtz r4, TARGET IF
0x100
                           ID
                                ΕX
                                    ME
                                        WB
0x104
       sub r4, r2, r5
                                            WB
0x108 \text{ sw } 0(r2), r1
                                IF
                                        EX
                                            ME
                                                WB
       and r6, r1, r8
0x10c
                                        ID
                                            EX
                                                ME
                                                    WB
0x110
       or r12, r13, r14
           TARGET = 0x200
TARGET: #
0x200 xor r9, r4, r11
                                            ID
                                               EX ME
                                                        WB
```

Branch is taken yet two instructions past delay slot (sub) complete execution.

Branch target finally fetched in cycle 4.

Problem: Two instructions following delay slot.

Handling Instructions Following a Taken Branch Delay Slot

Option 1: Don't fetch them.

```
Possible (with pipelining) because ...
... fetch starts (sw in cycle 2) ...
... after branch decoded.

(Would be impossible ...
... for non-delayed branch.)
```

```
IF ID EX ME WB

NPC

25:21 Addr Data rsv

20:16 Addr Data rtv

Addr Din rtv

Addr Din Out

NPC

Addr Din Out

Addr Din Out

NPC

Addr Din Out

NPC
```

```
#I Adr
                Cycle
                                                         8
0x100
       bgtz r4, TARGET IF
                                 EX
                                     ME
                                         WB
                            ID
      sub r4, r2, r5
0x104
                            \operatorname{IF}
                                 ID
                                     EX
                                         ME
                                             WB
       sw 0(r2), r1
0x108
                                 IF
                                         EX
                                             ME
                                                 WB
       and r6, r1, r8
0x10c
                                     IF
                                         ID
                                             EX
                                                 ME
                                                     WB
0x110
      or r12, r13, r14
           TARGET = 0x200
TARGET: #
0x200 xor r9, r4, r11
                                                 EX ME
                                                         WB
```

Handling Instructions Following a Taken Branch

Option 2: Fetch them, but squash (stop) them in a later stage.

This will work if instructions squashed ...

... before modifying architecturally visible storage (registers and memory).

Memory modified in ME stage and registers modified in WB stage . . .

... so instructions must be stopped before beginning of ME stage.

Can we do it? Depends depends where branch instruction is.

In example, need to squash sw before cycle 5.

During cycle 3 bgtz in ME ...

... it has been decoded and the branch condition is available ...

... so we know whether the branch is taken ...

... so sw can easily be squashed before cycle 5.

Option 2 will be used.

Instruction Squashing

In-Flight Instruction::

An instruction in the execution pipeline.

Later in the semester a more specific definition will be used.

```
Squashing:: [an instruction]
preventing an in-flight instruction . . .
. . . from writing registers, memory or any other visible storage.
```

Squashing also called: nulling, abandoning, and cancelling..

Like an insect, a squashed instruction is still there (in most cases) but can do no harm.

Squashing Instruction in Example MIPS Implementation

Two ways to squash.

• Prevent it from writing architecturally visible storage.

Replace destination register control bits with zero. (Writing zero doesn't change anything.)

Set memory control bits (not shown so far) for no operation.

• Change Operation to nop.

Would require changing many control bits.

Squashing shown that way here for brevity.

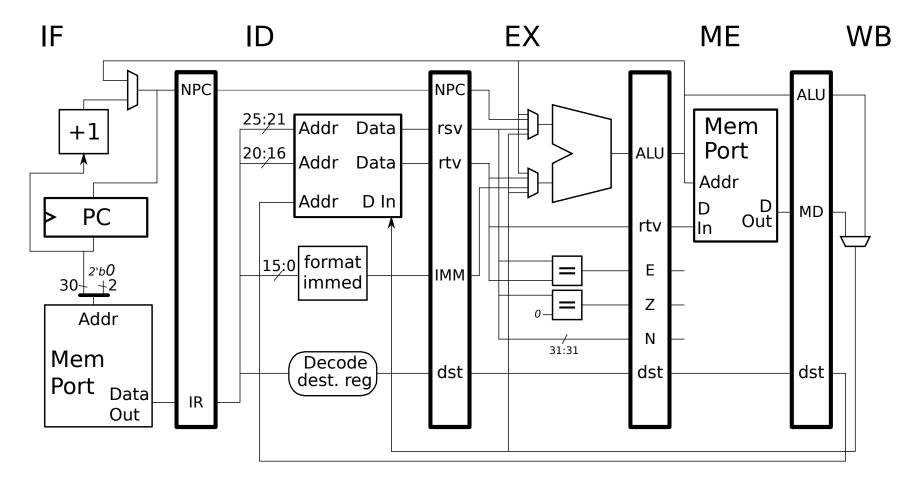
Illustrated by placing a nop in IR.

Why not replace squashed instructions with target instructions?

Because there is no straightforward and inexpensive way to get the instructions where and when they are needed.

(Curvysideways and expensive techniques covered in Chapter 4.)

MIPS implementation used so far.



Example of correct execution

```
#I Adr
                 Cycle
                                               5
                                                    6
                                                            8
                                           4
0x100
       bgtz r4, TARGET IF
                                  \mathsf{EX}
                                      ME
                                           WB
                             ID
0x104 sub r4, r2, r5
                              \operatorname{IF}
                                  ID
                                      EX
                                           ME
                                               WB
       sw 0(r2), r1
0x108
                                  IF
                                      IDx
0x10c
       and r6, r1, r8
                                      IFx
0x110 or r12, r13, r14
TARGET: #
           TARGET = 0x200
0x200 xor r9, r4, r11
                                               ID
                                                       ME
                                                            WB
```

Branch outcome known at end of cycle 2 . . .

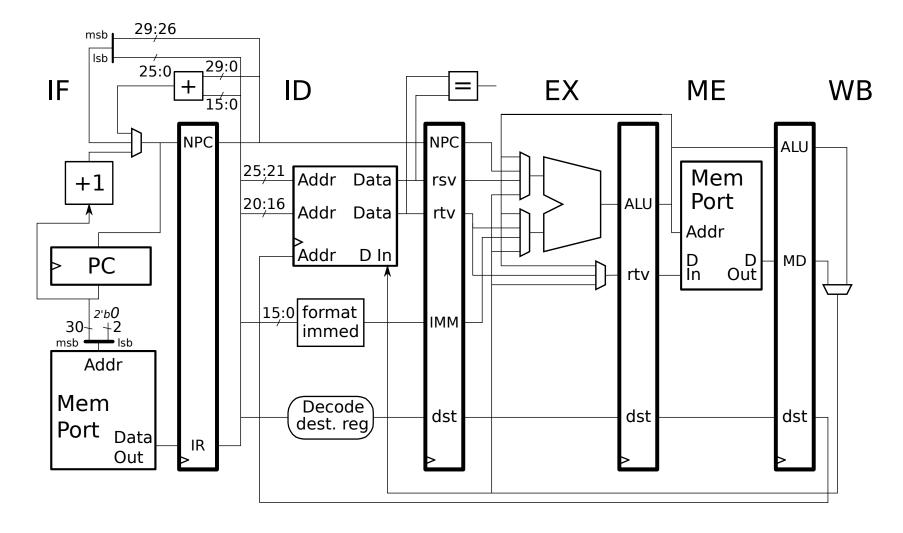
- ... wait for cycle 3 when doomed instructions (sw and and) in flight
- ... and squash them so in cycle 4 they act like nops.

Two cycles (2, and 3), are lost.

The two cycles called a branch penalty.

Two cycles can be alot of cycles, is there something we can do?

Zero-Cycle Branch Delay Implementation



Compute branch target address in ID stage.

Branch Hardware » Zero-Cycle Branch Delay Implementation

Compute branch target and condition in ID stage.

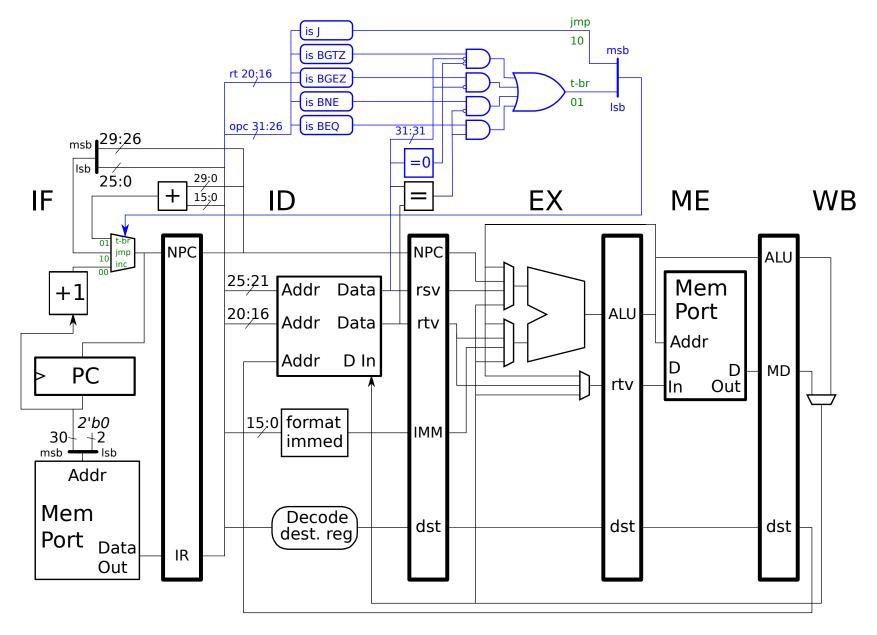
Workable because register values not needed to compute branch address and branch condition can be computed quickly.

Now how fast will code run?

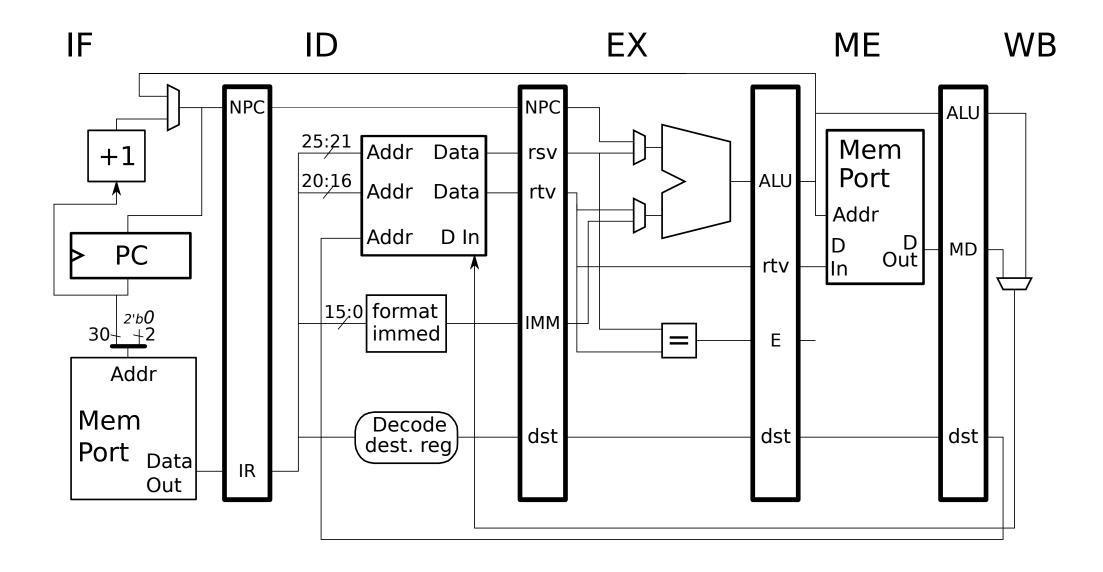
```
#I Adr
                Cycle
                                                          8
0x100 bgtz r4, TARGET IF
                                 EX
                            {	t ID}
                                         WB
0x104 sub r4, r2, r5
                             IF
                                 ID
                                     EX
                                         ME
                                             WB
0x108 sw 0(r2), r1
0x10c and r6, r1, r8
0x110 or r12, r13, r14
TARGET: #
           TARGET = 0x200
0x200 xor r9, r4, r11
                                 \operatorname{IF}
                                     ID
                                         EX ME
                                                 WB
```

No penalty, not a cycle wasted!!

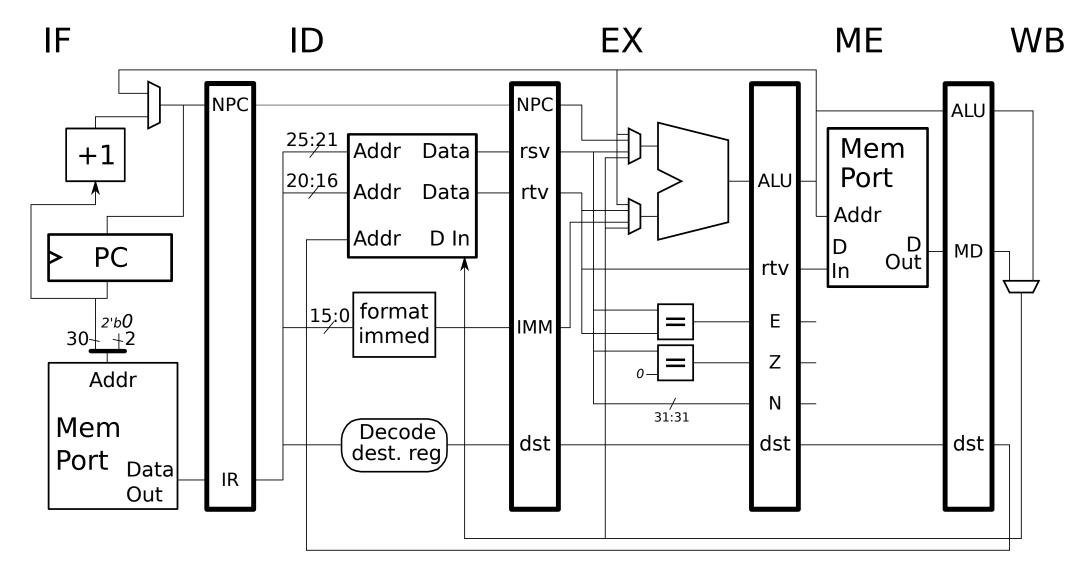
Control Logic for some Control Transfers



Non-Bypassed MIPS



Bypassed MIPS



ID Branch MIPS

