

Homework # 5 solution

In this HW

~~Problem 1~~ Here I will denote winter i
by w_i and ~~winter i~~

by M_i

Problem 1

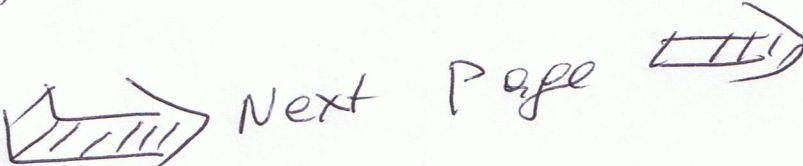

(a) we have: $F = \sum_{A, B, C, D} (0, 2, 4, 6, 9, 11, 13, 14, 15)$

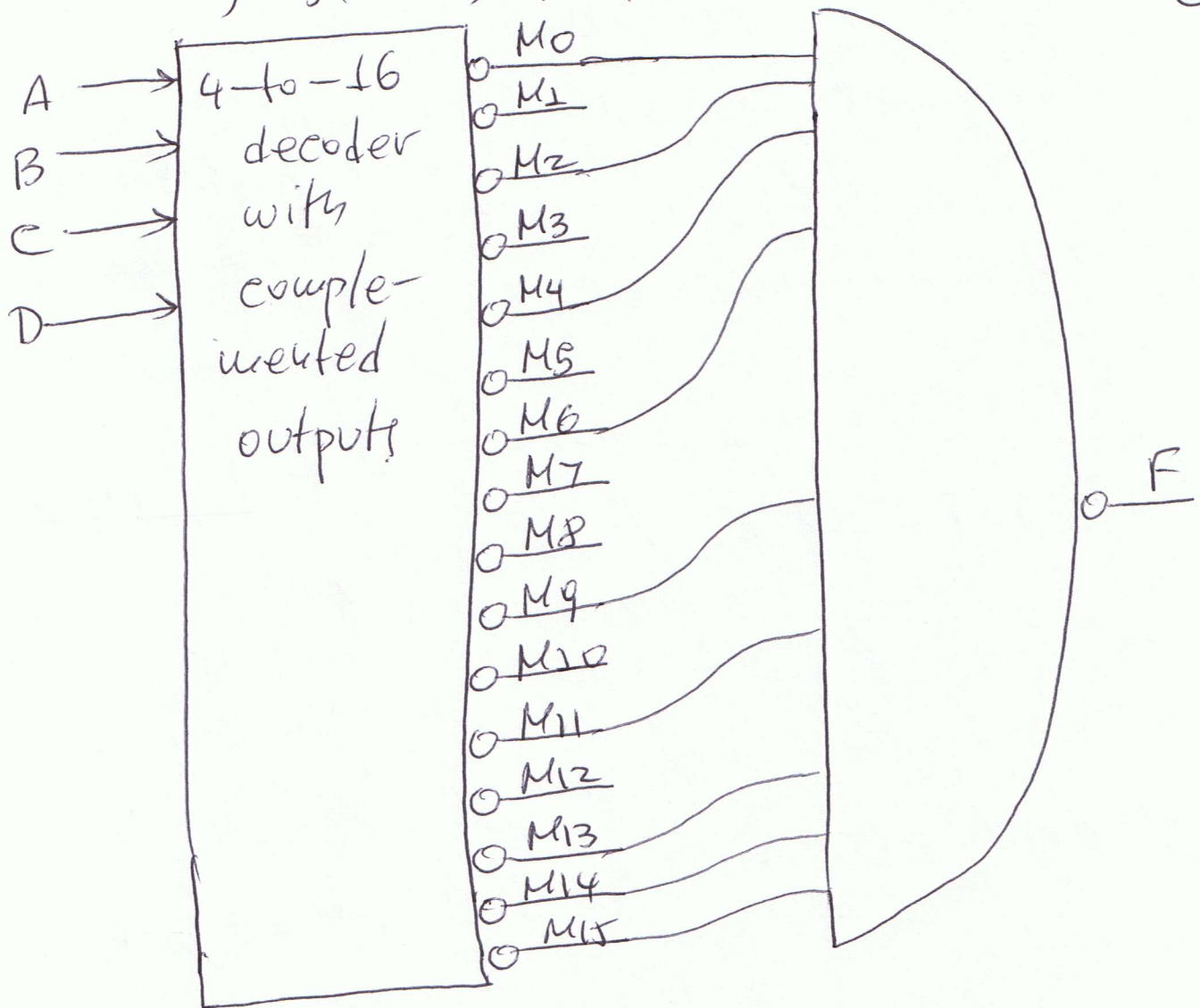
$$= m_0 w_2 + m_4 + w_6 + w_9 + w_{11} + w_{13} + m_{14} + w_{15}$$

$$= (m_0 \cdot w_2 \cdot w_4 \cdot w_6 \cdot w_9 \cdot w_{11} \cdot w_{13} \cdot m_{14} \cdot w_{15})'$$

$$= (M_0 \cdot M_2 \cdot M_4 \cdot M_6 \cdot M_9 \cdot M_{11} \cdot M_{13} \cdot M_{14} \cdot M_{15})'$$

From the above we get the figure
shown on the next page

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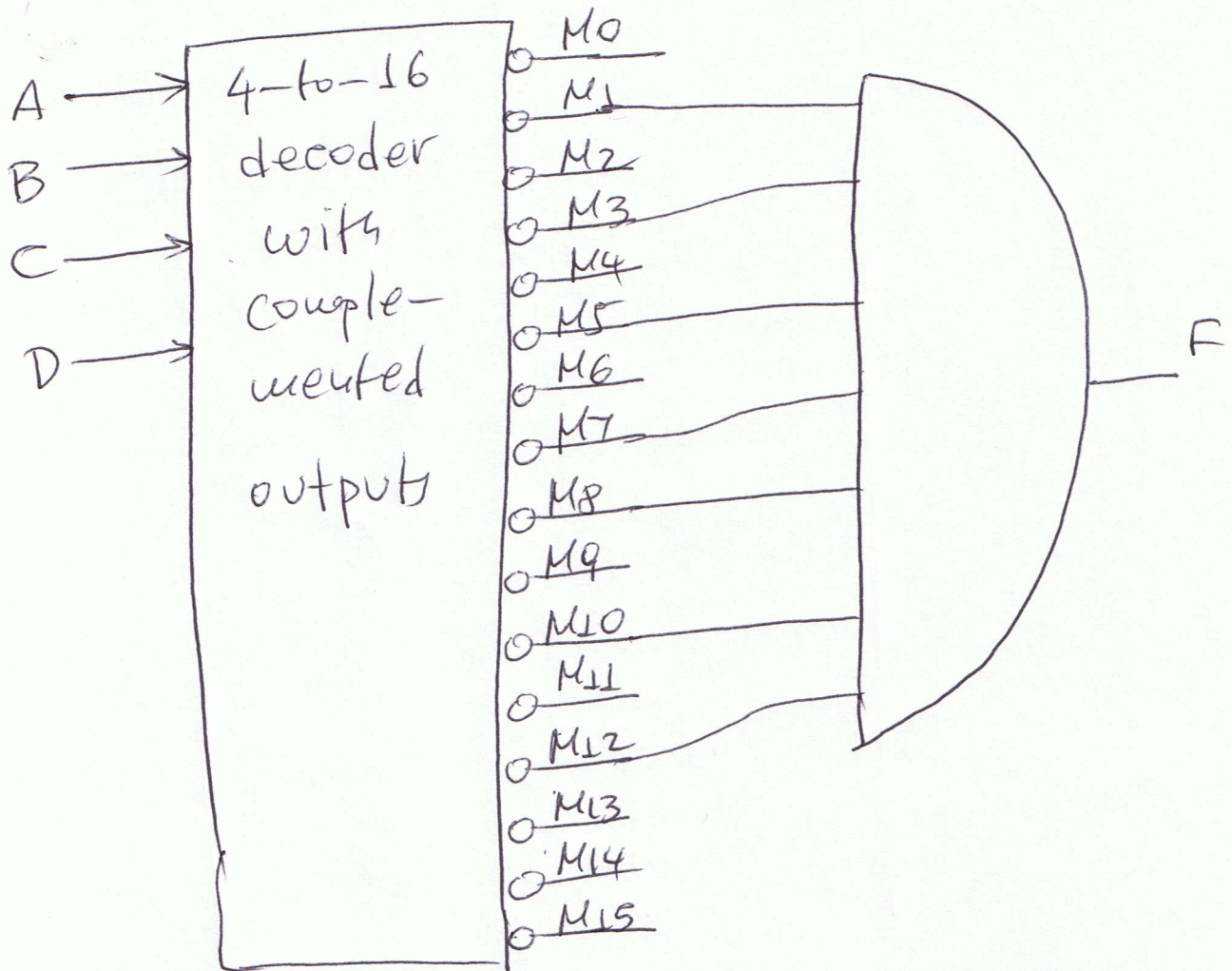
(b) we have:

$$F = \sum_{A, B, C, D} (0, 2, 4, 6, 9, 11, 13, 14, 15)$$

$$= \prod_{A, B, C, D} (1, 3, 5, 7, 8, 10, 12)$$

From the above we get the figure shown on the next page.

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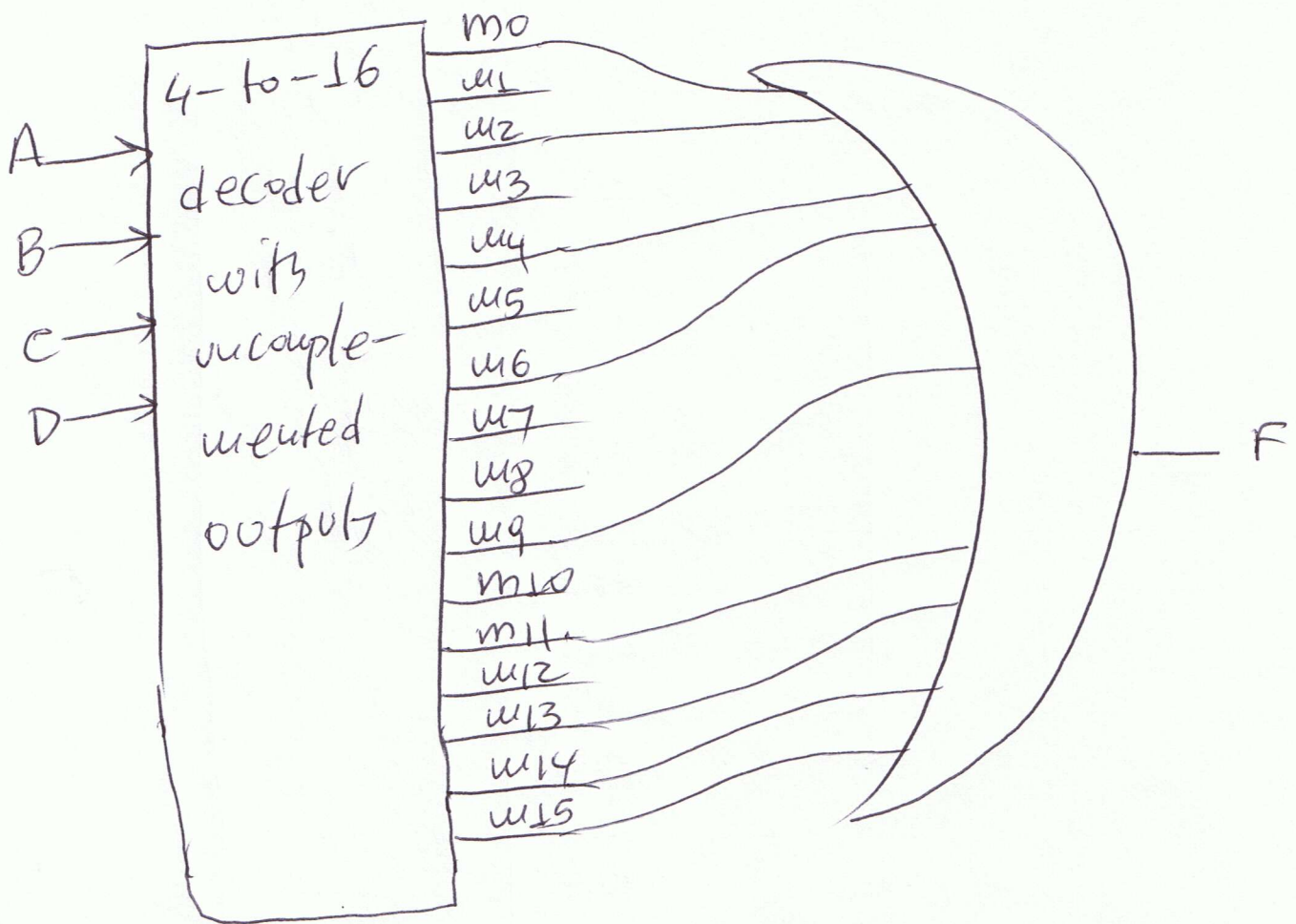


© we have

$$F = \sum_{A,B,C,D} (0, 2, 4, 6, 9, 11, 13, 14, 15)$$

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(d) we have:

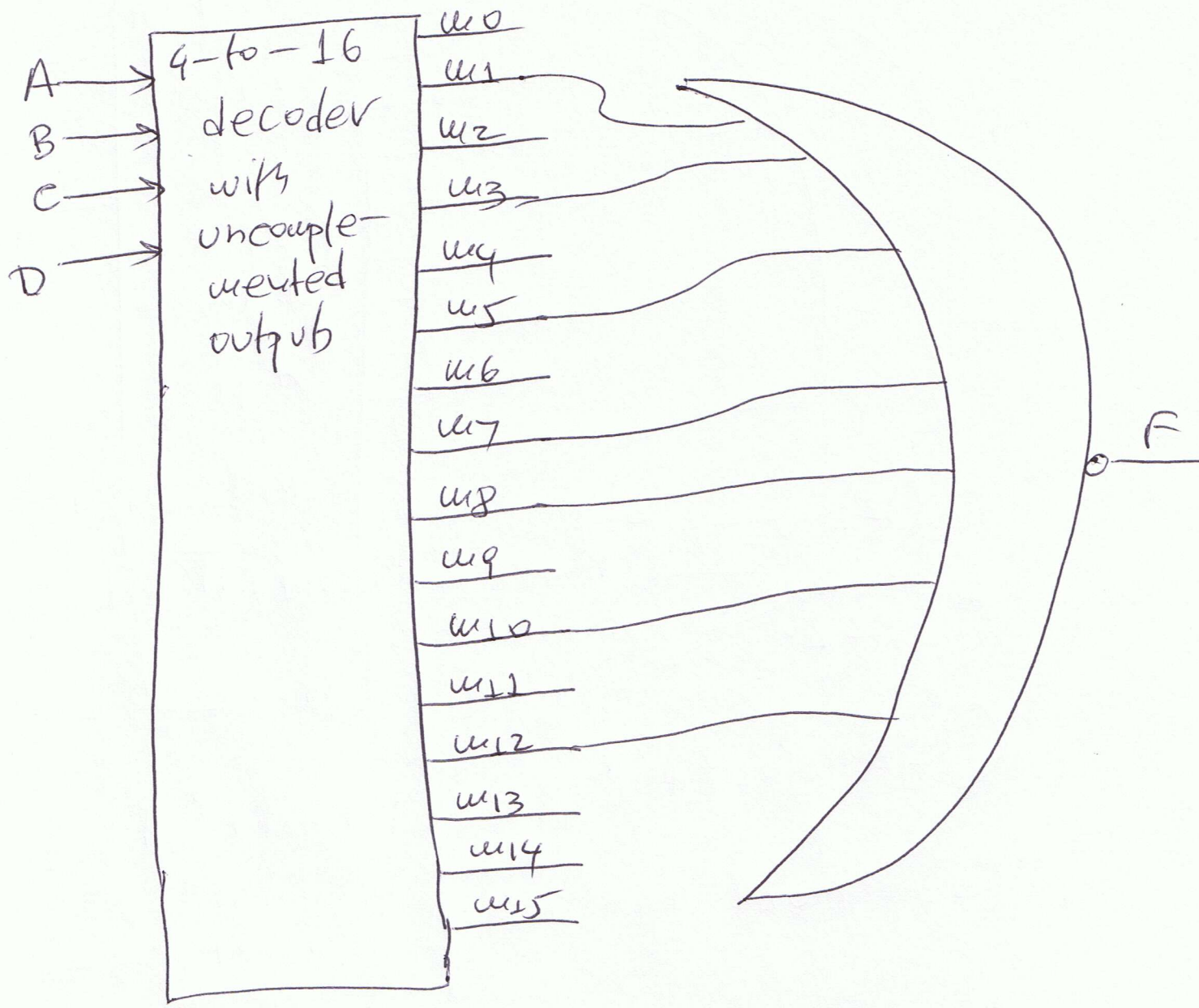
$$F = \prod_{A,B,C,D} (1, 3, 5, 7, 8, 10, 12)$$

$$= m_1 \cdot m_3 \cdot m_5 \cdot m_7 \cdot m_8 \cdot m_{10} \cdot m_{12}$$

$$= (m_1' + m_3' + m_5' + m_7' + m_8' + m_{10}' + m_{12}')'$$

$$= (m_1 + m_3 + m_5 + m_7 + m_8 + m_{10} + m_{12})'$$

From the above we get the figure shown on next page



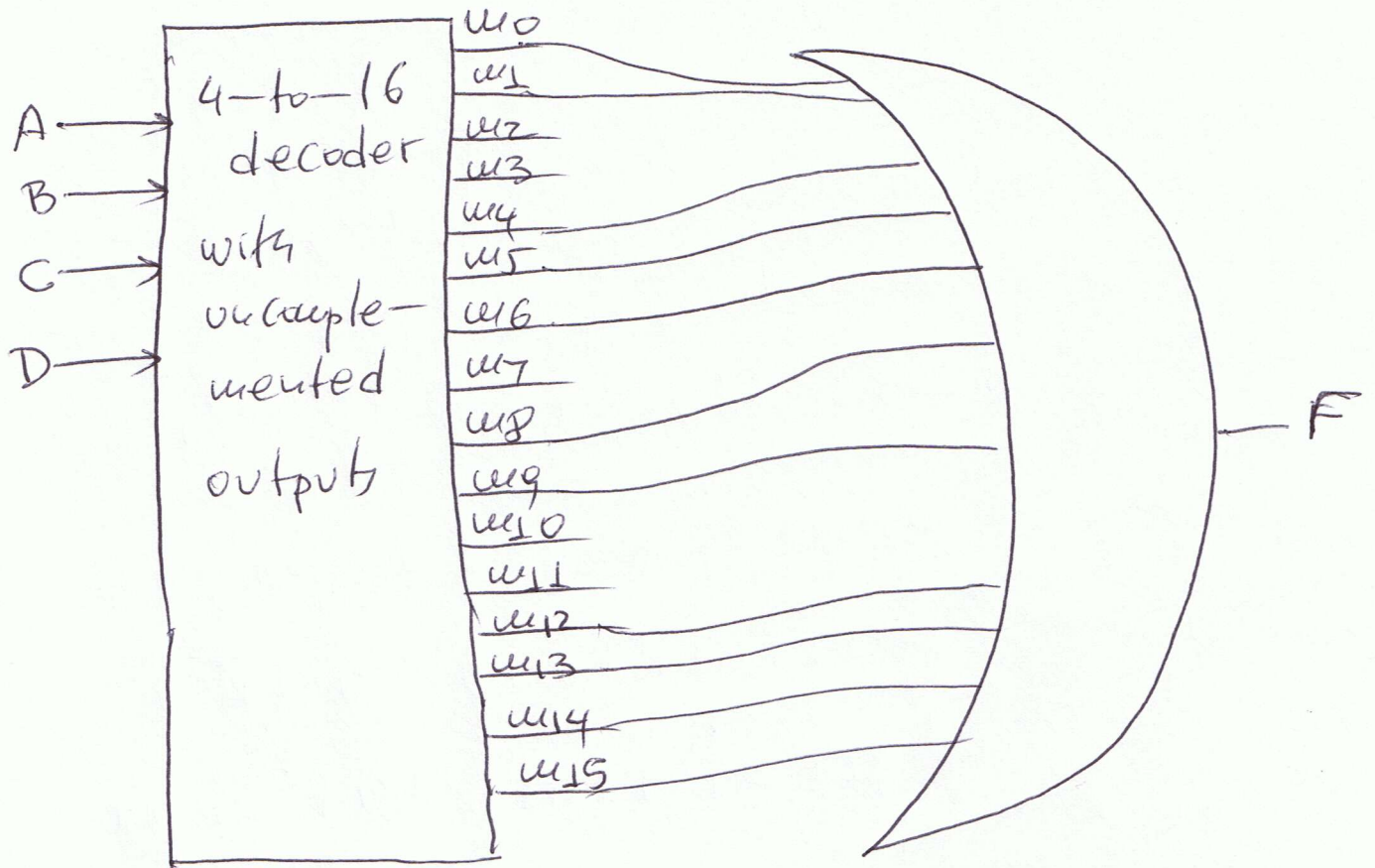
Problem 2: Since a decoder with uncomplemented outputs generates the minterms, we have to express F as a canonical sum. Since F is given as a product-of-sums expression, it is easier to obtain the canonical product from which we can easily get the canonical sum. We have

$$\begin{aligned}
 F &= (A' + B + C') \cdot (B + C' + D) \cdot (A + C' + D') \\
 &= \cancel{(A' + B + C' + D \cdot D')} \cdot \cancel{(A' + B + C')} \\
 &= (A' + B + C' + D \cdot D') \cdot (B + C' + D + A \cdot A') \cdot (A + C' + D' + B \cdot B') \\
 &= (A' + B + C' + D) \cdot (A' + B + C' + D') \cdot \\
 &\quad (B + C' + D + A) \cdot (B + C' + D + A') \\
 &\quad (A + C' + D' + B) \cdot (A + C' + D' + B') \\
 &= \begin{pmatrix} A' & B & C' & D \\ \downarrow & \circ & \downarrow & \circ \end{pmatrix} \cdot \begin{pmatrix} A' & B & C' & D' \\ \downarrow & \circ & \downarrow & \downarrow \end{pmatrix} \cdot \begin{pmatrix} A & B & C' & D \\ \circ & \circ & \downarrow & \circ \end{pmatrix} \\
 &\quad \begin{pmatrix} A' & B & C' & D \\ \downarrow & \circ & \downarrow & \circ \end{pmatrix} \cdot \begin{pmatrix} A & B & C' & D' \\ \circ & \circ & \downarrow & \downarrow \end{pmatrix} \cdot \begin{pmatrix} A & B' & C' & D \\ \circ & \downarrow & \downarrow & \downarrow \end{pmatrix} \\
 &= \prod_{A, B, C, D} (3, 3, 7, 10, 11) \Rightarrow \text{next page}
 \end{aligned}$$

Pr. 2 cont:

$$= \sum_{A, B, C, D} (0, 1, 4, 5, 6, 8, 9, 12, 13, 14, 15)$$

we now have

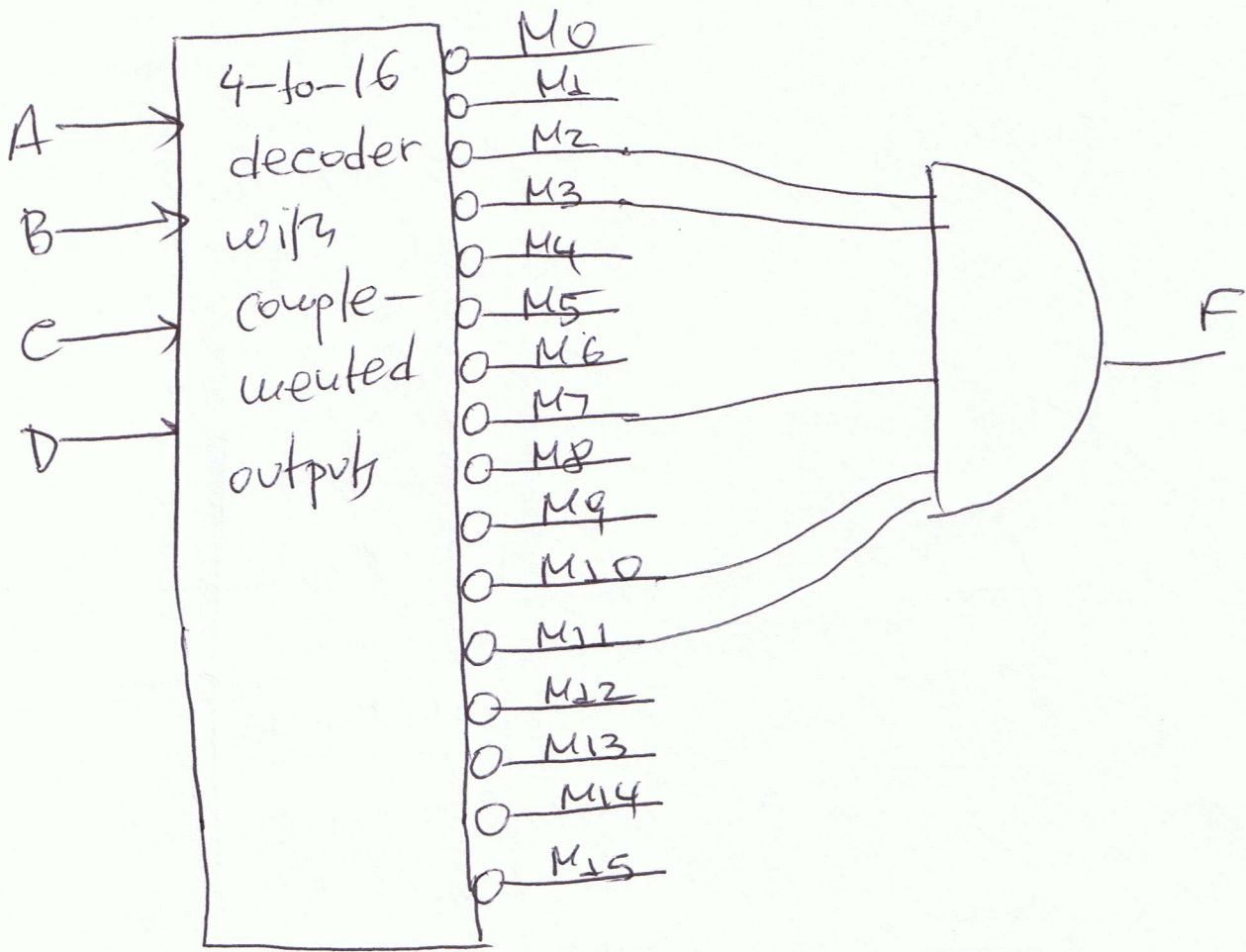


Pr. 3: From problem 2 we found out

$$\text{that } F = \prod_{A, B, C, D} (2, 3, 7, 13, 11)$$

We thus have the figure of next page

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Problem 4: Since a decoder with complemented outputs generates the minterms, we have to express F as a canonical product. Since F is given as sum-of-products, it is easier to obtain ~~the~~ ~~canonical sum~~ the canonical sum from which we can easily get the canonical product. We have:

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Pr. 4 cont:

$$F = A' \cdot B \cdot C' + B \cdot C' \cdot D + A \cdot C' \cdot D'$$

$$= A' \cdot B \cdot C' \cdot (D + D') + B \cdot C' \cdot D (A + A') \\ + A \cdot C' \cdot D' \cdot (B + B')$$

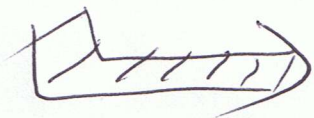
$$= \underset{\substack{0 & 1 & 0 & 1}}{A' \cdot B \cdot C' \cdot D} + \underset{\substack{0 & 1 & 0 & 0}}{A' \cdot B \cdot C' \cdot D'} + \underset{\substack{1 & 1 & 0 & 1}}{A \cdot B \cdot C' \cdot D}$$

$$+ \cancel{\underset{\substack{0 & 1 & 0 & 1}}{A' \cdot B \cdot C' \cdot D}} + \underset{\substack{1 & 1 & 0 & 0}}{A \cdot B \cdot C' \cdot D'} + \underset{\substack{1 & 0 & 0 & 0}}{A \cdot B' \cdot C' \cdot D'}$$

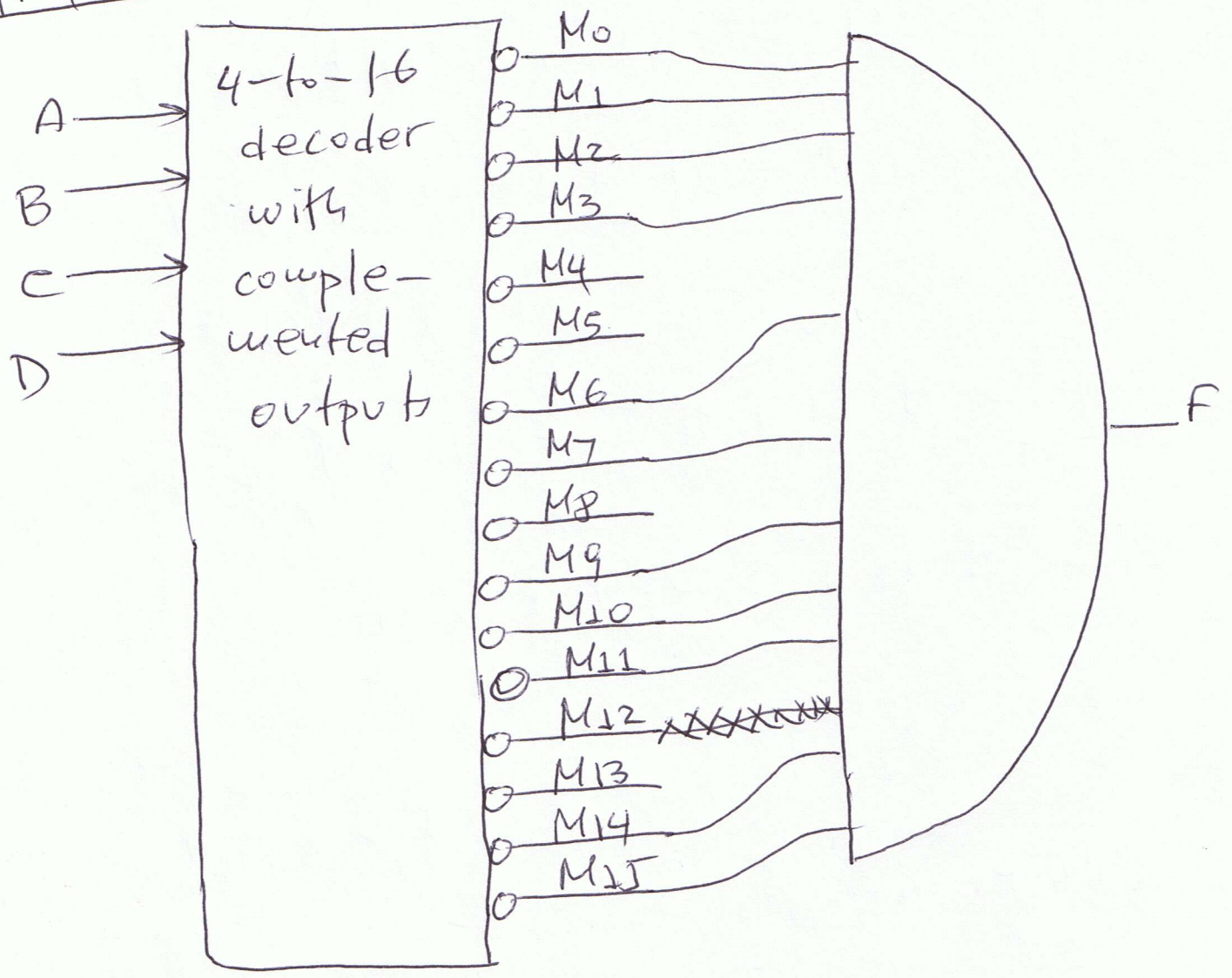
$$= \sum_{A, B, C, D} (4, 5, 8, 12, 13)$$

$$= \prod_{A, B, C, D} (0, 1, 2, 3, 6, 7, 9, 10, 11, 14, 15)$$

From the above we get the figure shown on next page



Pr. 4 cont.



Problem 5: From problem 4 we found

out that $F = \sum_{A,B,C,D} (4, 5, 8, 12, 13)$

we thus have the figure shown on next page

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Pr. 5 cont:

