

EE 3755

Fall 2002

HW# 1 Solutions

EE 3755, HW#1 Solutions (1)

⊥ Here the two numbers  $X$  and  $Y$  are of different signs and  $X+Y$  needs to be performed. We thus perform the following subtraction:

$$(\text{magnitude of } X) - (\text{mag. of } Y) = (11100) - (11110)$$

$$= (11100) + 2^2 \text{ compl. of } (11110) =$$

$$= 11100$$

$$+ \begin{array}{r} 00010 \\ \hline 011110 \end{array}$$

$\hookrightarrow c=0 \Rightarrow \text{result} < 0 \Rightarrow (\text{mag. of } X) - (\text{mag. of } Y) < 0$   
 $\Rightarrow \text{mag. of } X < \text{mag. of } Y.$

Therefore, sign bit of result = sign bit of  $Y = 1$   
 and magnitude of  $(X+Y) = 2^2 \text{ compl. of } (11110)$   
 $= (00010)$ . Thus  $X+Y = (100010)_2 = (-2)_{10}$ .

2 Here  $n=6$ , multiplier =  $(-27)_{10} = (100101)_2$ ; multiplicand =  $(-22)_{10} = (101010)_2$

Since three bits are to be examined at a time, the field B (left of multiplier field) must be of length  $6+1=7$  bits

Initialization 

B	A	d
0000000	100101	0

+ 1101010

010 → add 1x mult/cand and then do 2-bit right shift

1101010	100101	0
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result of 1<sup>st</sup> cycle

1111010	101001	0
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+ 1101010

010 → add 1x mult/cand and do 2-bit right sh.

1100100	101001	0
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result of 2<sup>nd</sup> cycle

1111001	001010	0
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+ 0101100

100 → add -2x mult/cand and do 2-bit right shift

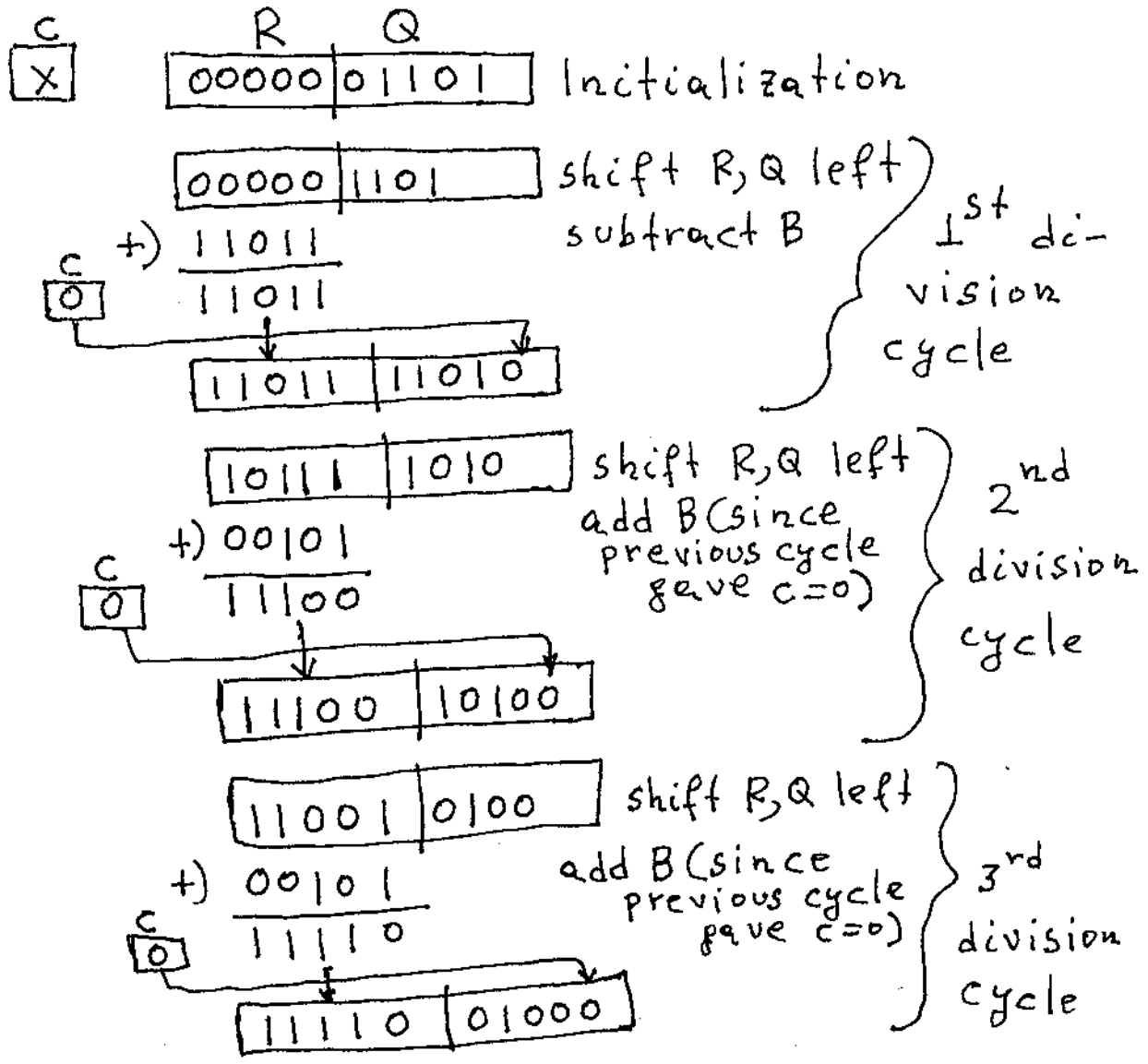
0100101	001010	0
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0001001	010010	1
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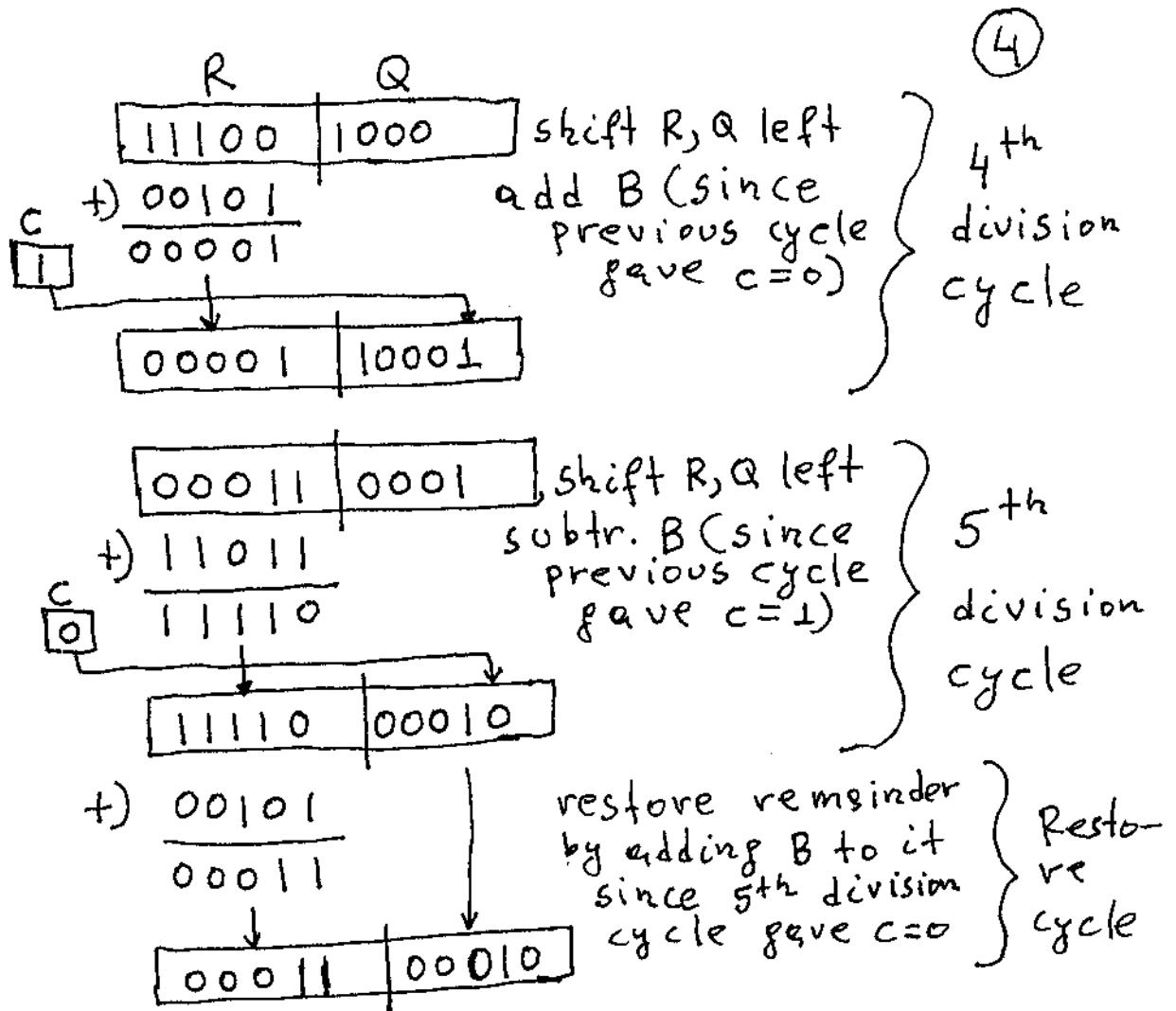
product =

$$= (001001010010)_2 = 594 = (-22) \times (-27)$$

3 Here the dividend is  $A = (0000001101)_2$   
 $= (+13)_{10}$ ; the divisor is  $B = (0010)_2 =$   
 $= (+5)_{10}$  and  $n = 5$ . Also,  $-B = 2$ 's comple-  
 ment of  $B = (11011)_2$

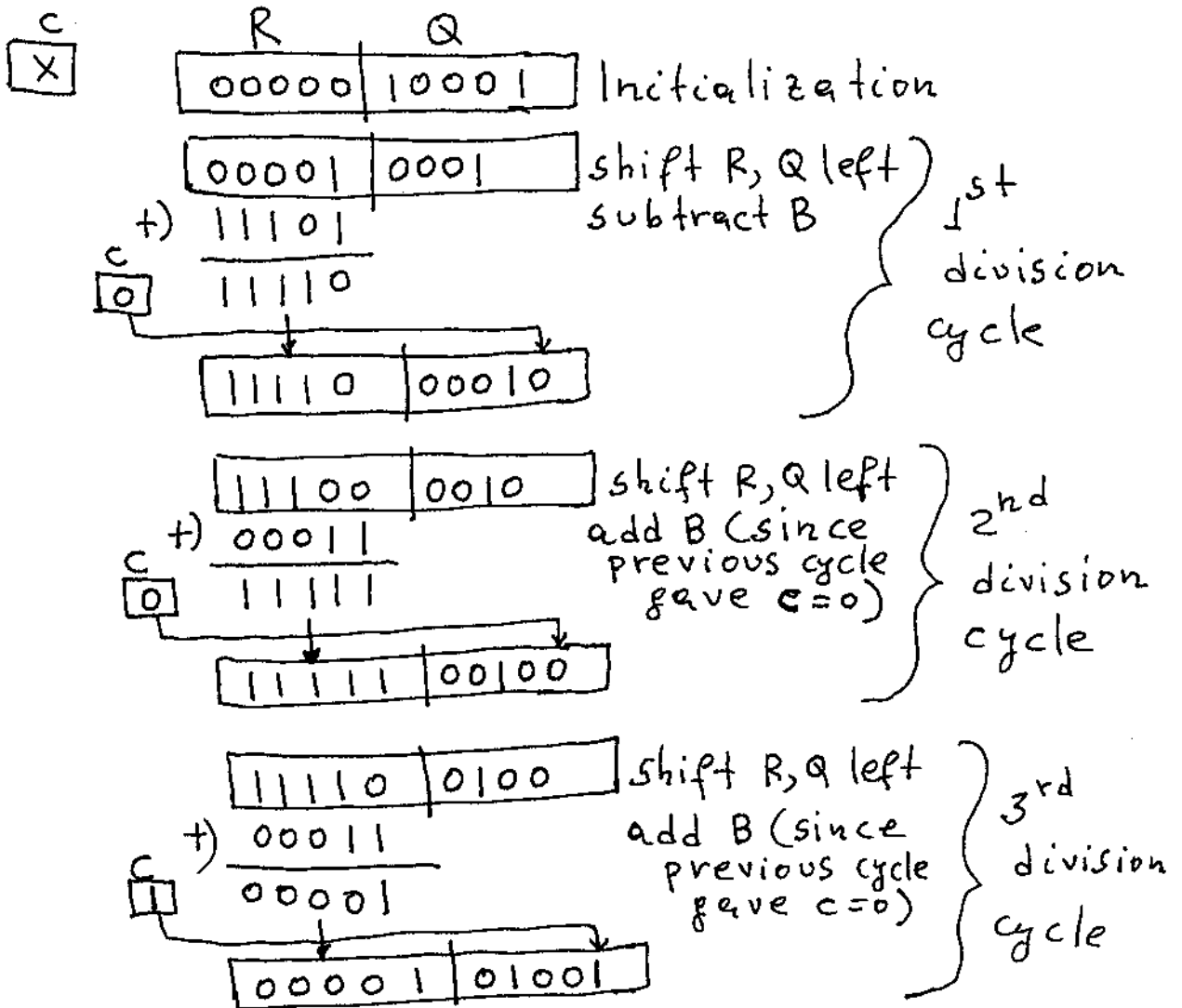


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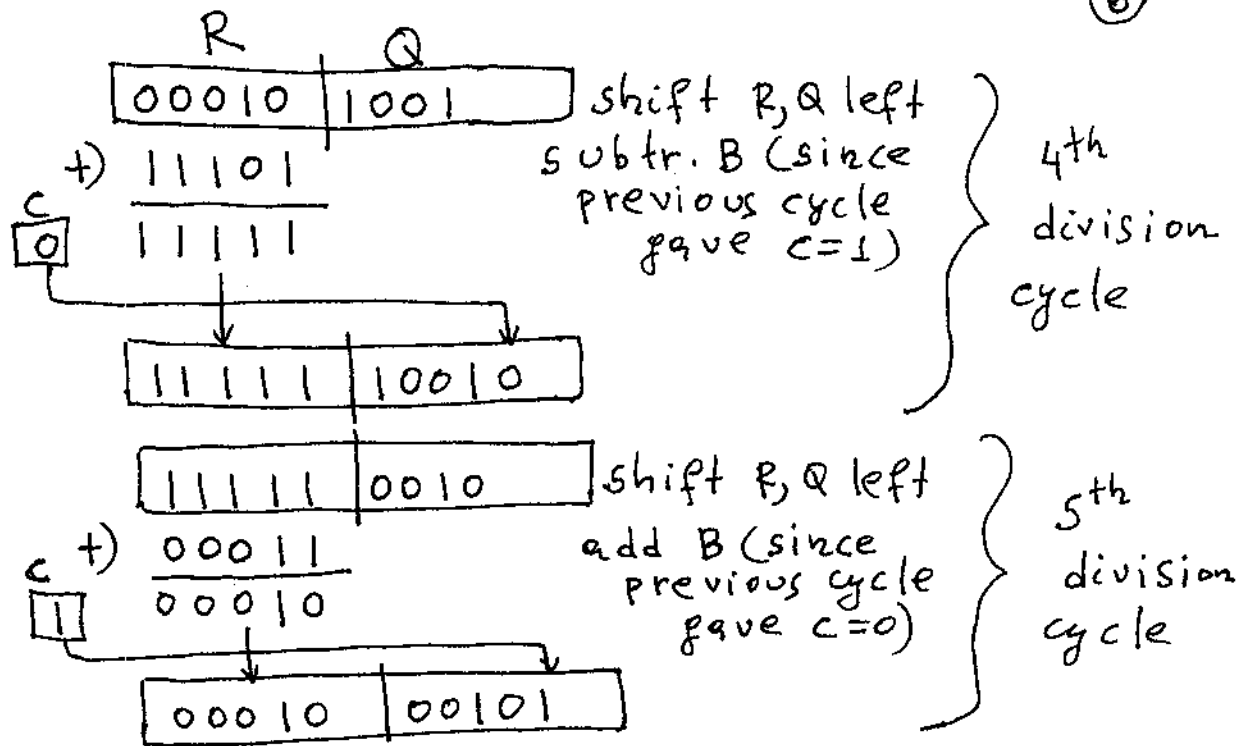
So remainder is  $R = (00011)_2 = 3$  while quotient is  $Q = (00010)_2 = 2$ . Double check to see that  $B \times Q + R = 5 \times 2 + 3 = 13 = A$

4 Here the dividend is  $A = (0000010001)_2 = (+17)_{10}$ ; the divisor is  $B = (00011)_2 = (+3)_{10}$  and  $n = 5$ . Also,  $-B = 2$ 's complement of  $B = (11101)_2$ .



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No restore cycle is necessary since the carry out of the 5th division cycle is 1. Here remainder is  $R = (00010)_2 = 2$  while quotient is  $Q = (00101)_2 = 5$ . Double check to see that  $B \times Q + R = 3 \times 5 + 2 = 17 = A$ .

5 The range of the fraction is

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$$0.5 \leq f \leq 1 - 2^{-29}$$

The range of the exponent is

$$-2^9 \leq e \leq 2^9 - 1 \quad \text{or} \quad -512 \leq e \leq 511$$

Thus the positive FLP dynamic range is

$$0.5 \times 2^{-512} \leq A^+ \leq (1 - 2^{-29}) \times 2^{511}$$

The negative FLP dynamic range is

$$-(1 - 2^{-29}) \times 2^{511} \leq A^- \leq -0.5 \times 2^{-512}$$

6 1. Align/adjust

$$e_1 - e_2 = e_1 + 2^s \text{ complement of } e_2 =$$

$$= 0111$$

$$+ 0111$$

$$\hline 01110$$

$$\begin{aligned} \rightarrow c=0 &\Rightarrow e_1 - e_2 < 0 \Rightarrow e_1 < e_2 \text{ and } e_2 - e_1 \\ &= 2^s \text{ complement of } (1110) = (0010)_2 = (2)_{10} \end{aligned}$$



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Thus  $A_1$  becomes

$$A_1: \begin{array}{|c|c|c|} \hline s_1 & e_2 & f_1' \\ \hline 0 & 1001 & 00111100 \\ \hline \end{array}$$

## 2. Subtract fractions

Since  $A_1$  and  $A_2$  are of different signs and  $A_1 + A_2$  needs to be performed, a subtraction must take place.

$$f_1' - f_2 = f_1' + 2^s \text{ complement of } f_2 =$$

$$\begin{array}{r} \cdot 00111100 \\ +) \cdot 01101110 \\ \hline 0 \cdot 10101010 \end{array}$$

$\hookrightarrow c=0 \Rightarrow f_1' - f_2 < 0 \Rightarrow f_1' < f_2$ . Since

$f_2$  is the larger fraction, the result

$A_3 = A_1 + A_2$  must have as a sign bit the sign bit of  $A_2$  (negative sign).

The fraction of  $A_3 = A_1 + A_2$  will be the 2's complement of  $(10101010) = 01010110$

Therefore

$$A_3: \begin{array}{|c|c|c|} \hline 1 & 1001 & 01010110 \\ \hline \end{array}$$

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### 3. Postnormalize

After postnormalization we get

$$A_3: \begin{array}{|c|c|c|} \hline s_3 & e_3 & f_3 \\ \hline 1 & 1000 & 10101100 \\ \hline \end{array}$$

### 4. Check for exponent underflow

No exponent underflow occurred.

See that  $e_3 = (1000)_2 = 8 \in [0, 15]$

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a

$$G_5^* = G_{23} + G_{22} \cdot P_{23} + G_{21} \cdot P_{22} \cdot P_{23} + G_{20} \cdot P_{21} \cdot P_{22} \cdot P_{23}$$

$$b) P_6^* = P_{27} \cdot P_{26} \cdot P_{25} \cdot P_{24}$$

$$c) C_{23} = G_5^* + G_4^* \cdot P_5^* + G_3^* \cdot P_4^* \cdot P_5^* + G_2^* \cdot P_3^* \cdot P_4^* \cdot P_5^* \\ + G_1^* \cdot P_2^* \cdot P_3^* \cdot P_4^* \cdot P_5^* + G_0^* \cdot P_1^* \cdot P_2^* \cdot P_3^* \cdot P_4^* \cdot P_5^* \\ + C_{-1} \cdot P_0^* \cdot P_1^* \cdot P_2^* \cdot P_3^* \cdot P_4^* \cdot P_5^*$$

$$d) C_{26} = G_{26} + G_{25} \cdot P_{26} + G_{24} \cdot P_{25} \cdot P_{26} + \\ ~~G_{23} \cdot P_{24} \cdot P_{25} \cdot P_{26}~~ C_{23} \cdot P_{24} \cdot P_{25} \cdot P_{26}$$